

## ERRATA

Correction to

### A CYCLIC INEQUALITY AND A RELATED EIGENVALUE PROBLEM

J. L. SEARCY AND B. A. TROESCH

Volume 81 (1979), 217-226

Professor P. Nowosad, Rio de Janeiro, has informed us that the inequality  $S(x) \geq N/2$  holds for  $N = 12$  [1]. Furthermore, our belief that the inequality also holds for odd  $N \leq 23$  has been stated, and strongly supported by numerical evidence, in [2].

1. E. K. Godunova and V. I. Levin, *A cyclic sum with 12 terms*, Mathematical Notes of the Academy of Sciences of the USSR, **19** (1976), 510-517. (translation), Consultants Bureau, New York.
2. P. J. Bushell and A. H. Craven, *On Shapiro's cyclic inequality*, Proc. Royal Soc. Edinburgh, 75A, **26** (1975/76), 333-338.

Corrections to

### CHARACTERIZATION OF A CLASS OF TORSION FREE GROUPS IN TERMS OF ENDOMORPHISMS

E. F. CORNELIUS, JR.

Volume 79 (1978), 341-355

Received February 5, 1974 and in revised form June 7, 1978.

Corrections to

### NONOPENNESS OF THE SET OF THOM-BOARDMAN MAPS

LESLIE C. WILSON

Volume 84 (1979), 225-232

In [3] we showed that the set of Thom-Boardman maps is open if the Morin  $(S_{1;k})$  singularities alone occur generically, and is not

open if  $S_2$  singularities occur generically. However, we neglected to consider the  $S_{1,i}$  singularities,  $i \geq 2$  (recall that the subscripts denote corank, not kernel rank, and that  $S_{1;k}$  means  $S_{1,1,\dots,1}$  with  $k$  1's). In fact, the set of Thom-Boardman maps is not open if the  $S_{1,2}$  singularities occur generically, which occurs whenever  $n > p \geq 4$ . Thus Theorem 1.1 of [3] should be stated: The Thom-Boardman maps form an open subset of  $C(N, P)$  iff either  $2p > 3n - 4$  or  $p < 4$ .

We will now indicate how the above claims are proved. Using Proposition 3 of [2], it is easy to calculate that the codimension of  $S_{1,2}$  (which Mather denotes  $\Sigma^{n-p+1,2}$ ; we assume  $n > p$ ) is  $n - p + 4$ . Thus  $S_{1,2}$  singularities occur generically iff  $n > p \geq 4$ .

The 3-jet at 0 of

$$f(x_1, \dots, x_n) = (x_1, \dots, x_{p-1}, x_p^2 + \dots + x_{n-2}^2 + x_{n-1}^2 x_n \\ + x_1 x_{n-1} + x_2 x_n + x_3 x_n^2)$$

lies in  $S_{1,2,0} \cap {}_t S_{1,2}$ . That it lies in  $S_{1,2,0}$  follows from Mather's algorithm for computing the Thom-Boardman type (see the last definition on p. 236 of [2]). That  $j^2 f$  is transverse to  $S_{1,2}$  follows from the last paragraph in [2].

For each  $k$ ,  $z = j^k f(0)$  lies in the closure of  $S_{1;k}$ . To see this, note that the contact class of  $x^2 y + Q$ ,  $Q$  a nondegenerate quadratic form in other variables, lies in the closure of the contact class of  $x^2 y - y^k + Q$  (consider the curve  $x^2 y - t y^k + Q$ ). By Table 3 of [1], the latter contact class lies in the closure of the contact class of  $x^2 + y^{k+1} + Q$ , which lies in  $S_{1;k}$ .

By the Transversal Extension Theorem of [3], there is a Thom-Boardman map  $g$  with  $j^k g(0) = z$ . By Lemma 3.5 of [3], there are maps  $g_m$  which converge to  $g$  in the Whitney  $C^\infty$  topology such that each  $g_m$  has  $S_{1;k}$  singularities. The codimension of  $S_{1;k}$  is  $n - p + k$ . Thus, choosing  $k > p$ ,  $g_m$  cannot be a Thom-Boardman map.

#### REFERENCES

1. J. Callahan, *Singularities and plane maps II: sketching catastrophes*, Amer. Math. Monthly, **84** (1977), 765-803.
2. J. Mather, *On Thom-Boardman Singularities, Dynamical Systems*, Academic Press, New York, 1973.
3. L. Wilson, *Non-openness of the set of Thom-Boardman maps*, Pacific J. Math.