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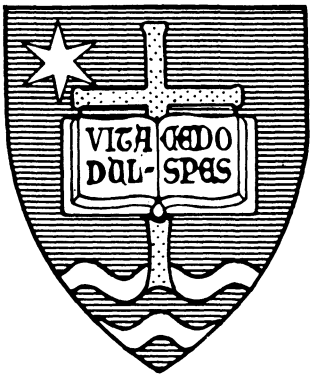

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Authors should consult the "Guide to authors" for editorial information. Articles and editorial correspondence should be sent to *B. Sobociński, Editor, P.O. Box 28, Notre Dame, Indiana 46556, U.S.A.*

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