

E. Vidal Abascal. *Introduccion a la geometria diferencial*. Madrid, Editorial Dossat, 1956, 16+329 pp. 220 ptas.

This book, written by the professor of geometry at the University of Santiago de Compostela, is a textbook of classical differential geometry with the usual subjects. In its use and notation of vectors, its general treatment of material and problems it acknowledges the influence of reviewers text *Lectures on classical differential geometry* (Cambridge, Mass., 1950), now also available in a Spanish translation by Bravo Gala: *Geometria diferencial clásica* (Madrid, Aguilar, 1955, 11+256 pp.). It contains, moreover, an introduction on vectors, determinants, matrices, and a special chapter on curves in the euclidean plane with some problems on isometry and integral geometry. In the discussion of these problems, as well as in the exposition of Cartan's methods in the theory of Pfaffians, the author acknowledges the influence of Blaschke's books on Differential and on Integral geometry; and in his preface pays tribute to Bieberbach's *Differentialgeometrie* (1932). We can also, in the text, make the acquaintance of some of Professor Vidal Abascal's own contributions to geometry. Among the many illustrations we find some pictures of the creators of differential geometry.

D. J. STRUIK

*Champs de vecteurs et de tenseurs*. By E. Bauer. Paris, Masson, 1955. 204 pp. 2200 fr.

This text treats three main topics: the elementary theory of vectors and tensors and applications, the more advanced theory of vectors and tensors, an introduction to electromagnetic theory. In the first two topics, the theories of vectors and tensors are presented simultaneously by skillfully interweaving both subjects. First, the customary intuitive approach for three-dimensional Euclidean space is given and in the advanced theory a more detailed study in affine and metric  $n$ -dimensional space is presented. The introduction to electromagnetic theory furnishes the basic ideas of this subject.

After defining vectors as directed line segments which add by the parallelogram law and discussing the scalar product, the author examines rectangular and oblique Cartesian coordinates and transformations of coordinates. This leads to Gibbs dyads and the introduction of tensors in terms of their components. Other topics in this section are: vector algebra, differentiation theory, and the theorems of Gauss and Stokes. In treating the last topic, the author uses the physical approach to interpret the divergence and curl of a vector

field and then defines these quantities as limits of integrals. The study of the del operator and Laplacian and Newtonian fields concludes this section of the text.

Vectors and tensors in affine and metric  $n$ -dimensional space are treated in Chapter IV. First, the author discusses the curl of a vector and the divergence of a vector density in affine  $n$ -space. This is followed by a discussion in metric space of the metric tensor, the absolute derivative, geodesics, and related topics.

Finally, the author considers the following topics in electromagnetic theory: electrostatic fields (force, energy, and polarization); electric currents (steady and non-steady) and the laws of Kirchoff, Joule, and Ampère; magnetic and electromagnetic fields. The last topic is presented with considerable skill and ranges from the Maxwell laws of classical three-dimensional Euclidean space (presented by classical vector methods) to the Lorentz-Einstein transformation in Minkowski space and the Maxwell tensor of relativity.

The level of the text is such that a mathematically mature student with a background in classical physics can follow the developments. The book should be of particular interest to physicists and engineers.

N. COBURN

*Surface area.* By L. Cesari. (Annals of Mathematics Studies, no. 35.) Princeton University Press, 1956. 10+595 pp. \$8.50.

The length  $l(C)$  of a curve  $C$  is the limit of the lengths  $l(p_n)$  of inscribed polygons  $p_1, \dots, p_n, \dots$  such that the maximum side-length of  $p_n$  converges to zero as  $n \rightarrow \infty$ . Almost eighty years ago, Schwarz and Peano noted that the analogous statement for surface area (in terms of the elementary areas of inscribed polyhedra) is false even in the simple case when the surface under consideration is the lateral surface of a circular cylinder. Subsequently, many other phenomena were noted which revealed further fundamental discrepancies between arc length and surface area. The immediate issue raised by the initial observations of Schwarz and Peano was, however, the formulation of a logically consistent definition of surface area. During the past eighty years, many such definitions have been proposed, and an enormous amount of effort has been expended in the study of these various concepts of surface area. As far as mathematical fields of a classical type are concerned, the reassuring inference from these studies is the fact that in reasonably decent cases the classical integral formula taught in calculus does indeed yield the correct value of surface area. On the other hand, the need for a comprehensive general theory of surface area became apparent