

# THE ANNALS of STATISTICS

AN OFFICIAL JOURNAL OF  
THE INSTITUTE OF MATHEMATICAL STATISTICS

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(Organized September 12, 1935)

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