

# THE ANNALS *of* STATISTICS

*AN OFFICIAL JOURNAL OF*  
THE INSTITUTE OF MATHEMATICAL STATISTICS

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