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The Annals of Probability, Volume 10, Number 3, August 1982. Published in February, May, August, and November by The Institute of Mathematical Statistics, IMS Business Office, 3401 Investment Blvd., Suite 6, Hayward, California 94545.

Mail to the *Annals of Probability* should be addressed to the Treasurer at the IMS Business Office as described above. It should not be addressed to Waverly Press.

Printed at the
WAVERLY PRESS, INC., BALTIMORE, MARYLAND 21202 U.S.A.

Second-class postage at Hayward, California and at additional mailing offices

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Beginning with the calendar year 1982, the two journals of The Institute of Mathematical Statistics will be printed quarterly. The total numbers of pages per volume will be approximately the same as before. Months of publication for 1982 are as follows.

Annals of Probability: February, May, August and November

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THE ANNALS OF PROBABILITY

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