

ERRATUM TO “GRAFTING, PRUNING, AND THE ANTIPODAL MAP ON MEASURED LAMINATIONS”

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Theorem 9.3 of [D] is incorrect; in the proof, the quadrilateral comparison cannot be applied directly to estimate the integral (7). However a weaker estimate follows by correcting the proof: one must use $|\|f_*v\|^2 - \|h_*v\|^2| = |\|f_*v\| - \|h_*v\|| \|\|f_*v\| + \|h_*v\|\|$ and the Cauchy-Schwarz inequality, bounding the resulting terms by the energy difference and the total energy of f and h , respectively. This method was used by Korevaar-Schoen in [KS] (see the proof of Proposition 2.6.3) to obtain a more general estimate of the difference of pullback metrics for maps to NPC spaces, from which the following replacements for Theorem 9.3 and Corollary 9.4 of [D] follow:

Theorem 9.3. *Let $f \in W^{1,2}(X, Y)$ where $X, Y \in \mathcal{T}(S)$ and Y is given the hyperbolic metric ρ . Let h be the harmonic map homotopic to f . Then*

$$\|f^*(\rho) - h^*(\rho)\|_1 \leq \sqrt{2} (\mathcal{E}(f) - \mathcal{E}(h))^{\frac{1}{2}} \left(\mathcal{E}(f)^{\frac{1}{2}} + \mathcal{E}(h)^{\frac{1}{2}} \right)$$

and in particular

$$\|\Phi(f) - \Phi(h)\|_1 \leq \sqrt{2} (\mathcal{E}(f) - \mathcal{E}(h))^{\frac{1}{2}} \left(\mathcal{E}(f)^{\frac{1}{2}} + \mathcal{E}(h)^{\frac{1}{2}} \right).$$

Theorem 9.4. *Let $f \in W^{1,2}(\tilde{X}, T_\lambda)$ be a π_1 -equivariant map, where $X \in \mathcal{T}(S)$ and $\lambda \in \mathcal{ML}(S)$. Then*

$$\|\Phi(f) + \frac{1}{4}\phi_X(\lambda)\|_1 \leq \sqrt{2} (\mathcal{E}(f) - \mathcal{E}(\pi_\lambda))^{\frac{1}{2}} \left(\mathcal{E}(f)^{\frac{1}{2}} + \mathcal{E}(\pi_\lambda)^{\frac{1}{2}} \right)$$

The main results of [D] are unaffected by these changes, since they are asymptotic in nature and the proofs only require bounds that are $o(\mathcal{E}(h))$ when $\mathcal{E}(f) - \mathcal{E}(h) = O(1)$ and $\mathcal{E}(h) \rightarrow \infty$. Only Theorem 10.1 must be revised; we have instead:

Theorem 10.1. *Let $X \in \mathcal{T}(S)$ and $\lambda \in \mathcal{ML}(S)$. Then the Hopf differential $\Phi_X(\lambda)$ of the collapsing map $\kappa : X \rightarrow \text{pr}_\lambda X$ and the Hubbard-Masur differential $\phi_X(\lambda)$ satisfy*

$$\|4\Phi_X(\lambda) - \phi_X(\lambda)\|_1 \leq C \left(1 + E(\lambda, X)^{\frac{1}{2}} \right)$$

where $E(\lambda, X)$ is the extremal length of λ on X and C is a constant depending only on $\chi(S)$.

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References

- [D] D. Dumas, *Grafting, pruning, and the antipodal map on measured laminations*, J. Differential Geom. **74**(1) (2006) 93–118, MR 2260929.
- [KS] N.J. Korevaar & R.M. Schoen, *Sobolev spaces and harmonic maps for metric space targets*, Comm. Anal. Geom. **1** (1993) 561–659, MR 1266480, Zbl 0862.58004.

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