

## DISCUSSION OF “COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS”

BY FORREST W. CRAWFORD

*Yale School of Public Health*

I congratulate the authors on this valuable contribution to the statistics profession, and for their diligent work collecting the coauthorship and citation data sets upon which their analysis is based. The paper provides a valuable perspective on an important aspect of relationships between papers and between individual statisticians in a few of the most prominent journals in the field. The authors’ analyses of these relationships yields new insights, paves the way for future data collection efforts, and provides a valuable data set for further analytical exploration. In this brief discussion, I will give a few general comments and questions, and give suggestions for future work. I focus on three areas: author, paper and journal attributes, selection of authors and journals, and the role of time in the process of research collaboration and citation.

**1. The role of author, paper and journal attributes.** Collection of additional metadata, including paper content and author characteristics (current institution, department, Ph.D. institution, time since Ph.D., dissertation advisor, etc.), could potentially yield additional insight into the complex process of coauthorship and citation. The characteristics of authors themselves may be important. For example, what proportion of authors are students versus professors? Often the order of authorship matters: usually the first author did most of the work, and the last author is in charge. Middle authors have moderate contributions. How does author order arise from coauthorship arrangements? Is the more senior author usually the last author?

One might expect that coauthorship relationships are most common among authors who have been physically proximate in the past or currently. Coauthorship within the same institution might be most common. Is the same true for coauthorship in the same department? Can we learn about the collaborative character of academic statistics and biostatistics departments by studying the pattern of collaborations within and between them? Online access to scholarly publications, blogs and researcher websites have made it increasingly easy to identify potential collaborators all around the world. We might expect the prevalence of collaboration across large geographic distances to become more common as information barriers become less pronounced.

---

Received August 2016.

**2. The role of selection.** I am curious about whether the networks derived from the four journals analyzed in this paper can be used to give more general information about the broader network of statistical collaboration and citation. Like the other discussants Regueiro, Sosa and Rodríguez, I found the communities identified by the authors somewhat puzzling. As the authors say in their disclaimer, these clusters can be hard to interpret. One reason that the communities may not match with our heuristic expectations is the nature of subsampling in graphs.

To formalize ideas, let  $G = (V, E)$  be the full coauthor network of statisticians, however one might choose to define this group, where  $V$  is the set of statisticians and an edge in  $E$  indicates a coauthorship relationship. Let  $J$  be the set of statistics journals, however we might define it. For each edge  $\{i, k\} \in E$ , there is an associated set of journals  $J_{ik}$  in which  $i$  and  $k$  have coauthored at least one article. Of course,  $J_{ik} = \emptyset$  if  $i$  and  $k$  have never authored an article together.

Let  $H \subseteq J$  be a subset of journals. Suppose now that we find a subgraph  $G_H = (V_H, E_H)$  in which  $V_H$  consists of all authors that have published at least once in a journal in  $H$ , and  $\{i, k\} \in E_H$  if, for some  $j \in J_{ik}$ ,  $j \in H$ . Equivalently,  $G_H$  is the induced coauthorship subgraph of authors who have published at least once in the journal set  $H$ . This setup is essentially a model of selection on vertex attributes. Is the induced subgraph  $G_H$  “representative” of  $G$ ? Does it share any topological properties with  $G$ ? The answers to these questions speak directly to claims that the field is becoming more collaborative.

It is now well known that subsamples of networks can be troublesome [Chandrasekhar and Jackson (2014), Lee, Kim and Jeong (2006), Shalizi and Rinaldo (2013), Stumpf, Wiuf and May (2005)]. Since degree is not preserved by taking the induced subgraph from subsampled vertices, centrality measures—especially degree centrality—may not be preserved either. Transitivity, clustering and other network features of  $G_H$  may not be generalizable to  $G$ . Even if the journals in  $H$  were selected at random from  $J$ ,  $G_H$  still might not preserve some topological properties of  $G$ . In summary, it is possible that considering a different set  $H \subseteq J$  of journals would yield starkly different conclusions about collaboration.

**3. The role of time.** Coauthorship and collaboration are social processes that evolve over time, but the networks discussed in the paper are static. The authors suggest that the field of statistics has become more competitive, collaborative and globalized. In addition to their reliance on metadata not collected here, these assertions seem to indicate a role for time in the evolving pattern of interactions between authors. Associated with each paper in the data set is a publication date. Of course, publication date is not the same thing as the date of initiation of authorship, the date a manuscript is finished, or even the date it is accepted by the journal. But if we assume these journals have similar average review times, we can at least take the time ordering of publication to be a rough measure of the time order of paper authorship.

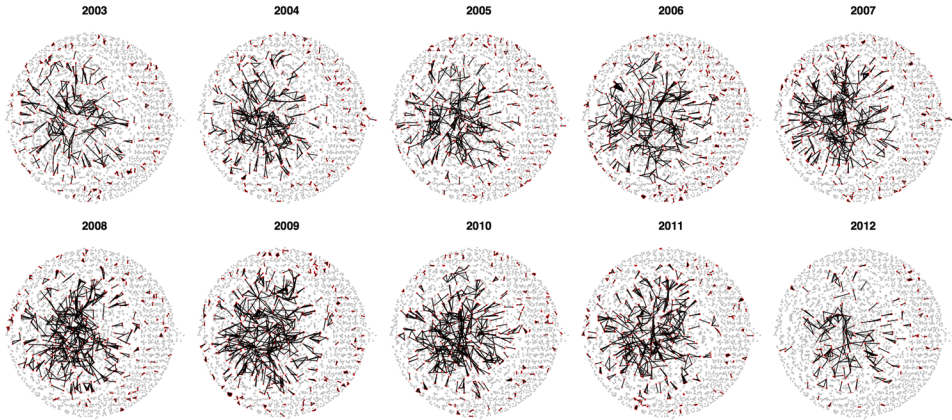


FIG. 1. Coauthorship network “B” by year. Vertices represent authors and edges represent coauthorship. Red vertices are authors who published at least one paper in that year. The vertex layout is the same from year to year.

In addition, edges and other apparent topological patterns in the multi-year coauthorship network correspond to discrete events, ordered in time. For example, a triangle  $(i, j, k)$  in the multi-year network may indicate three coauthors  $(i, j, k)$  of the same paper, or distinct coauthorship relationships  $(i, j)$ ,  $(j, k)$  and  $(i, k)$ , or some combination, at possibly different times. The time ordering of the papers represented by these edges likely matters in our interpretation of topological features of the network.

We can also understand the coauthorship data as a contact process between authors, and the citation data as a contact process between papers, rather than as networks [e.g., [Blundell, Beck and Heller \(2012\)](#), [Hawkes and Oakes \(1974\)](#)]. While authors exist before and after their publication of any particular paper, articles can only cite those that were previously published (or at least available in citable form). If the publication date of a paper  $i$  is  $t_i$ , then the citation data may be understood as a directed graph in which an edge from paper  $i$  to  $j$  can only occur if  $t_j < t_i$ .

Figure 1 shows Coauthorship network “B” by year. Red vertices represent authors of papers appearing that year in one of the journals, and gray vertices indicate authors in the data set who did not author a paper in those journals in that year. The layout of vertices in the graphs is the same from year to year. The central connected component seems to remain mostly constant in its density from year to year, but in 2012 density of coauthorships is markedly decreased.

## REFERENCES

- BLUNDELL, C., BECK, J. and HELLER, K. A. (2012). Modelling reciprocating relationships with Hawkes processes. In *Advances in Neural Information Processing Systems* 2600–2608.
- CHANDRASEKHAR, A. G. and JACKSON, M. O. (2014). Tractable and consistent random graph models. Technical report, National Bureau of Economic Research, Cambridge, MA.

- HAWKES, A. G. and OAKES, D. (1974). A cluster process representation of a self-exciting process. *J. Appl. Probab.* **11** 493–503. [MR0378093](#)
- LEE, S. H., KIM, P.-J. and JEONG, H. (2006). Statistical properties of sampled networks. *Phys. Rev. E* (3) **73** 016102.
- SHALIZI, C. R. and RINALDO, A. (2013). Consistency under sampling of exponential random graph models. *Ann. Statist.* **41** 508–535. [MR3099112](#)
- STUMPF, M. P. H., WIUF, C. and MAY, R. M. (2005). Subnets of scale-free networks are not scale-free: Sampling properties of networks. *Proc. Natl. Acad. Sci. USA* **102** 4221–4224.

DEPARTMENT OF BIOSTATISTICS  
YALE SCHOOL OF PUBLIC HEALTH  
60 COLLEGE ST.  
PO BOX 208034  
NEW HAVEN, CONNECTICUT 06510  
USA  
E-MAIL: [forrest.crawford@yale.edu](mailto:forrest.crawford@yale.edu)  
URL: <http://crawfordlab.io>