Estimation of HIV Burden through Bayesian Evidence Synthesis

Daniela De Angelis, Anne M. Presanis, Stefano Conti and A. E. Ades

Abstract. Planning, implementation and evaluation of public health policies to control the human immunodeficiency virus (HIV) epidemic require regular monitoring of disease burden. This includes the proportion living with HIV, whether diagnosed or not, and the rate of new infections in the general population and in specific risk groups and regions. Estimation of these quantities is not straightforward: data informing them directly are not typically available, but a wealth of indirect information from surveillance systems and ad hoc studies can inform functions of these quantities. In this paper we show how the estimation problem can be successfully solved through a Bayesian evidence synthesis approach, relaxing the focus on “best available” data to which classical methods are typically restricted. This more comprehensive and flexible use of evidence has led to the adoption of our proposed approach as the official method to estimate HIV prevalence in the United Kingdom since 2005.

Key words and phrases: Bayesian inference, evidence synthesis, graphical model, HIV, disease burden.

1. INTRODUCTION

The HIV disease is associated with serious morbidity, high costs of treatment and care, and, in developing countries, with significant mortality and a high number of potential years of life lost (Joint United Nations Programme on HIV/AIDS, 2010). Planning for care provision and for implementation and evaluation of public health policies to reduce transmission relies crucially on robust monitoring of disease burden. This burden includes the proportion (prevalence) living with HIV; the proportion of infections remaining undiagnosed; and the rate at which new infections occur (incidence), in both the general population and in specific groups at high risk of infection and in different locations. To acquire robust evidence on these quantities is not easy. The assessment of HIV prevalence is complicated by the absence of symptoms for a long time after infection. Incidence is even more difficult to measure, requiring, at least, longitudinal follow-up of uninfected individuals, with all the complications of cohort studies.

Devising appropriate methods for estimation of prevalence and incidence has generated a rich literature in the last 30 years (Brookmeyer, 2010, Presanis, 2010). For HIV prevalence “direct” methods have been particularly popular amongst the medical community (e.g., McGarrigle et al., 2006, Lyerla et al., 2006 and references therein) for their apparent transparency. The underlying idea is that the general population, of size $N$, is subdivided into $G$ nonoverlapping groups at different risk of acquiring HIV. Estimates of proportions $\rho_g$ of risk group $g$ ($g = 1, \ldots, G$) in the population are multiplied by estimates of the prevalence $\pi_g$ of HIV to produce a point estimate of the number of infected individuals $N\pi_g\rho_g$ in each group and in the population $N \sum_g \rho_g \pi_g = N \sum_g (\rho_g \pi_g \delta_g + \rho_g \pi_g (1 - \delta_g))$. 
2. BAYESIAN EVIDENCE SYNTHESIS

Let \( \theta = (\theta_1, \ldots, \theta_K) \) represent the parameter vector. Denote by \( y = (y_1, \ldots, y_n) \) a collection of \( n \geq K \) independent data items available for the estimation of \( \theta \). Each \( y_i \) provides either direct information on a single component \( \theta_k \) of \( \theta \) or indirect information, that is, on functional parameters, expressed in terms of one or more component(s) of \( \theta \). Denote by \( \psi_i = \psi_i(\theta) \) a generic function of \( \theta \), which may represent the identity function, that is, \( \psi_i = \theta_k \), a function of a single parameter \( \psi_i = \psi_i(\theta_k) \) or a function of multiple components of \( \theta \), \( \psi_i = \psi_i(\theta) \). Indicating by \( L_i(\psi_i(\theta); y_i) \) the likelihood contribution of \( y_i \) to the basic parameter vector \( \theta \), from the independence of the \( y_i \), the full data likelihood is \( L(\theta; y) = \prod_{i=1}^n L_i(\psi_i(\theta); y_i) \). From a Bayesian perspective, expressing the prior knowledge on \( \theta \) through a prior distribution \( p(\theta) \), inference is conducted on the basis of the posterior distribution \( p(\theta | y) \propto p(\theta)L(\theta; y) \), which summarises all information, both direct and indirect, on \( \theta \). Such a distribution fully reflects the uncertainty about \( \theta \), including sampling variability and parameter uncertainty, which automatically percolates through to any function of the basic parameters \( \theta \). Figure 1 provides a direct acyclic graph (DAG) (Lauritzen, 1996) representation of the generic formulation above and shows schematically the dependency between data and parameters as well as the flow of information within the system. Here stochastic “nodes” are represented by circles and observed “nodes” by squares. The basic parameters, in double circles, are given prior (possibly hierarchical) distributions. Solid arrows represent distributional assumptions, and dashed arrows indicate functional relationships. Note the examples of functional parameters that inform multiple components of \( \theta \), such as

\[
\begin{align*}
\theta_1 & \quad \cdots \quad \theta_k & \quad \theta_{k+1} & \quad \cdots & \quad \theta_K \\
\psi_1 & \quad \cdots \quad \psi_i & \quad \psi_{i+1} & \quad \cdots & \quad \psi_n \\
y_1 & \quad \cdots \quad y_i & \quad y_{i+1} & \quad \cdots & \quad y_n
\end{align*}
\]

Fig. 1. DAG representation of a generic evidence synthesis model.
\( \psi_i = \psi_i(\theta_1, \theta_k) \). Information flows along the arrows, from the prior and from the data. The posterior distribution of each \( \theta_k \) is based on its prior distribution and on direct and indirect information available on it, as well as the priors and information on other components of \( \theta \).

### 3. HIV Prevalence Estimation

Extending the notation introduced in Section 1, HIV prevalence \( \pi_{t,r} \) in the general population at a single point in time \( t \) in location \( r \) may be expressed as

\[
\pi_{t,r} = \sum_g \rho_{t,g,r} \pi_{t,g,r} = \sum_g \rho_{t,g,r} \pi_{t,g,r} \delta_{t,g,r} + \sum_g \rho_{t,g,r} \times \pi_{t,g,r}(1 - \delta_{t,g,r}).
\]

The aim is to estimate the basic parameters \( \theta_{t,g,r} = (\rho_{t,g,r}, \pi_{t,g,r}, \delta_{t,g,r}) \). Having obtained the posterior distribution of these, it is possible to obtain the posterior distribution of any function of interest, for example, the total number of infections \( N_{t,r} \), or the total number of undiagnosed infections \( \pi_{t,g,r}(1 - \delta_{t,g,r}) \).

#### 3.1 Data

Different types of data are available on the following: group sizes, HIV prevalence, prevalence of undiagnosed infections, proportion of infections diagnosed, total number of diagnosed infections and group distribution amongst diagnosed cases. Data sources are described in full and commented upon elsewhere (Goubar et al., 2008, Presanis et al., 2010 and references therein), and are only briefly reviewed here.

Mid-year population estimates provide information on \( N_{t,r} \) and some risk group proportions \( \rho_{t,g,r} \). The remaining \( \rho_{t,g,r} \) are derived from a behavioural survey. Unlinked anonymous sero-prevalence surveys amongst STI clinic attendees inform the prevalence of undiagnosed infection \( \pi_{t,g,r}(1 - \delta_{t,g,r}) \). The analogous surveys amongst pregnant women and IDUs inform prevalence \( \pi_{t,g,r} \) and proportion diagnosed \( \delta_{t,g,r} \), both directly for some groups and indirectly through functions of \( \pi_{t,g,r}, \delta_{t,g,r} \) and \( \rho_{t,g,r} \). The pregnant women’s survey, in particular, measures prevalence in those born in SSA and the remainder (NSSA). These NSSA are a mixture of STI clinic attendees, IDUs and lower risk women. The observed data, therefore, provide information on a complex function of HIV prevalence in these groups and account for the probability of each group being included in the sample. An annual cross-sectional survey of diagnosed individuals collects information on functional parameters representing both the total number living with diagnosed HIV \( (N_{t,r} \sum_g \rho_{t,g,r} \pi_{t,g,r} \delta_{t,g,r}) \) and the distribution of risk groups amongst these individuals \( ((\rho_{t,g,r} \pi_{t,g,r} \delta_{t,g,r})/(\sum_g \rho_{t,g,r} \pi_{t,g,r} \delta_{t,g,r})) \) for each group \( g \). Table 1 summarises the spread and the type

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Table 1: Relationship between available data and parameters for a generic location \( r \)
of information available as well as the relationship between the available data and the basic parameters, expressed here through generic functions $\psi$. Note the sparseness of information on heterosexual men and the multiplicity of data on heterosexual women.

### 3.2 Inference

**Sampling distributions.** Information $y_{t,g,r}$ from most sources can be expressed in the form of count data $x_{t,g,r}$ with an associated denominator $n_{t,g,r}$. These data can be assumed to naturally be realisations of a binomial random variable

$$X_{t,g,r} \sim \text{binomial}(n_{t,g,r}, \psi_{t,g,r}),$$

where $\psi_{t,g,r}$ equals any of $\rho_{t,g,r}$, $\pi_{t,g,r}$ and $\delta_{t,g,r}$ if $y_{t,g,r}$ provides direct information or is a function of these basic parameters.

The observed total numbers of diagnosed men and women in each location, $x_{t,m,r}$ and $x_{t,f,r}$, respectively, are assumed to be realisations of Poisson random variables $X_{t,m,r} \sim \text{Poisson}(\mu_{t,m,r})$ and $X_{t,f,r} \sim \text{Poisson}(\mu_{t,f,r})$, where

$$\mu_{t,m,r} = N_{t,m,r} \sum_{gm} (1 - v_{t,gm}) \delta_{t,gm,r} \pi_{t,gm,r} \rho_{t,gm,r},$$

$$\mu_{t,f,r} = N_{t,f,r} \sum_{gf} (1 - v_{t,gf}) \delta_{t,gf,r} \pi_{t,gf,r} \rho_{t,gf,r}.$$  

Here $g_m$ and $g_f$ refer to male and female groups, respectively, and $v_{t,gm}$, $v_{t,gf}$ are parameters representing potential bias in the reported number of diagnosed individuals due to nonattendance, under-reporting or duplication. The region-specific numbers diagnosed in each risk group, $x_{t,gm,r}$ and $x_{t,gf,r}$, are simultaneously drawn from gender-specific multinomial distributions with size parameters $\mu_{t,m,r}$ and $\mu_{t,f,r}$, and probability parameters

$$\xi_{t,gm,r} = (1 - v_{t,gm}) \delta_{t,gm,r} \pi_{t,gm,r} \rho_{t,gm,r} / \sum_{gm} (1 - v_{t,gm}) \delta_{t,gm,r} \pi_{t,gm,r} \rho_{t,gm,r},$$

$$\xi_{t,gf,r} = (1 - v_{t,gf}) \delta_{t,gf,r} \pi_{t,gf,r} \rho_{t,gf,r} / \sum_{gf} (1 - v_{t,gf}) \delta_{t,gf,r} \pi_{t,gf,r} \rho_{t,gf,r}.$$  

The full likelihood $L_t(\theta_t; y_t)$ results from the product of each of these distributions, as generically described in Section 2.

**Spariness of information.** One of the challenges to the “direct” methods is the lack of information on some risk groups. Table 1 clearly shows that data on $\pi_{t,g,r}$ and $\delta_{t,g,r}$ for male heterosexuals are sparse. This sparsity can be addressed by sharing information between men and women. Although $\pi_{t,g,r}$ and $\delta_{t,g,r}$ are expected to vary by gender and by location, it is reasonable to assume that their male-to-female odds ratios might be similar between regions. To borrow strength across locations and risk groups, the following hierarchical structures are then assumed for the male-to-female log odds ratios of prevalence $\lor.\pi_{t,g,r}$ and proportion diagnosed $\lor.\delta_{t,g,r}$:

$$\logit(\pi_{t,gm,r}) = \lor.\pi_{t,g,r} + \logit(\pi_{t,gf,r}),$$

$$\lor.\pi_{t,g,r} \sim \text{normal}(P_{t,g}, \sigma_{t,\pi}^2),$$

$$\logit(\delta_{t,gm,r}) = \lor.\delta_{t,g,r} + \logit(\delta_{t,gf,r}),$$

$$\lor.\delta_{t,g,r} \sim \text{normal}(D_{t,g}, \sigma_{t,\delta}^2),$$

with a further hierarchy over risk groups:

$$P_{t,g} \sim \text{normal}(\Pi_t, \omega_{t,\pi}^2), \quad D_{t,g} \sim \text{normal}(\Delta_t, \omega_{t,\delta}^2).$$

The means $\Pi_t$ and $\Delta_t$ are a priori distributed as $\text{normal}(0, 100^2)$. The standard deviations $\sigma_{t,\pi}$, $\sigma_{t,\delta}$ and $\omega_{t,\pi}$, $\omega_{t,\delta}$ are given informative priors expressing the belief that only 5% of region-specific male-to-female odds ratios (of both prevalence and proportion diagnosed) will vary from the mean by more than a 1.3 factor (Section 5.7.3 of Spiegelhalter, Abrams and Myles, 2004). The odds ratios for prevalence are assumed to vary more across risk groups than across regions, hence, the prior for $\omega_{t,\pi}$ is weaker: a factor of 1.6 is used.

**Bias modelling and other indirect information.** A further challenge to the estimation problem is represented by data that indirectly inform a specific parameter of interest. The most common example occurs where the data are known to be affected by biases, as for the above total number of diagnosed infections. The parameters $v_{t,gm}$ and $v_{t,gf}$ are, in this case, introduced to model the known bias. In general, this is dealt with by introducing “bias models” that take the generic form $\theta' = \theta + \varepsilon$ on a suitable scale, where $\theta$ is the parameter of interest and $\theta'$ is the parameter directly informed by the data. The “bias parameter” $\varepsilon$ is a measure of the discrepancy between $\theta'$ and $\theta$. Where information or expert opinion on the size and/or direction of the bias is available, this is expressed as an informative prior on $\varepsilon$. 


Other challenges in the data sources, such as greater spatial heterogeneity than is captured by the regional structure adopted in the model, are met by more complex modelling, such as mixed effects regression on a finer regional stratification. The parameters $\psi_{t,g,r}$ in the binomial expression above may therefore have a more complex functional structure than the examples given here; see Goubar et al. (2008), Presanis et al. (2008), Presanis (2010) for more details.

**Priors.** Diffuse uniform priors are chosen for the basic parameters $\pi_{t,g,r}$ and $\delta_{t,g,r}$. The proportions of the male and female populations in each risk group $\rho_{t,g,m,r}$ and $\rho_{t,g,f,r}$ are given Dirichlet priors such that they sum to 1. Informative normal or uniform priors are assigned to bias parameters such as $\nu_{t,g,m}$ and $\nu_{t,g,f}$.

**Results.** Samples from the posterior distribution are obtained using Markov chain Monte Carlo (MCMC), implemented in WinBUGS (Lunn et al., 2000). Posterior summaries are based on 8000 samples from two chains after convergence is achieved. Figure 2 presents the estimated number of HIV infections in E&W, by diagnosis status and risk group.

4. **JOINT PREVALENCE AND INCIDENCE MODEL**

Application of the prevalence model over successive years using a sequence of data sets $\{y_t\}, t \in 1, \ldots, T$, provides the joint posterior distribution of the proportions of the population $N_{t,g,r}$ in each of three compartments: susceptible to infection $s_{t,g,r} = \rho_{t,g,r} (1 - \pi_{t,g,r})$; HIV infected but undiagnosed $u_{t,g,r} = \rho_{t,g,r} \pi_{t,g,r} (1 - \delta_{t,g,r})$; and infected and diagnosed $d_{t,g,r} = \rho_{t,g,r} \pi_{t,g,r} \delta_{t,g,r}$. These can be interpreted as estimates of the state at time $t$ of a dynamical system describing the processes of infection and diagnosis. Such a system can be approximated by a continuous-time Markov model whose dynamics are described through a system of ordinary differential equations (ODEs). As in Presanis et al. (2011), we focus here on the MSM group and, for simplicity, drop the subscripts $g$ and $r$. Let $c_t = (s_t, u_t, d_t)$ and denote by $\lambda_t$ the transition rates in the time interval $[t, t+1)$, assumed piecewise constant over the interval. Using additional data $\{z_t\}$ (Presanis et al., 2011) and prior information on demographics and risk behaviour uptake, a joint prevalence and incidence model can be formulated to allow simultaneous estimation of the prevalence parameters $\theta_t$, the compartment proportions $c_t$.
and the transition rates $\lambda_t$, including $\lambda_t^{s,u}$, the incidence rate, that is, the rate at which susceptible individuals enter the infected state. The DAG in Figure 3 provides a schematic representation of this joint model. The proportions $c_{t+1}$ at time $t+1$ are defined, through the ODEs, in terms of the rates $\lambda_t$ during the period $[t, t+1)$ and the initial condition of the system at $t=1$. The prevalence parameters $\theta_t$ and $\lambda_t$ govern the prevalence and rate data, respectively. Note that this DAG has the same structure as that in Figure 1. Now the $\lambda_t$ and $c_t$ are the basic parameters and the $\theta_t$ are functional parameters.

Inference is conducted as described in Section 2. The likelihood of the joint data is

$$L(c_1, \lambda; y, z) = \prod_{t=1}^{T} L_t(c_1; y_t)L_t(\lambda_t; z_t),$$

where $L_t(c_1; y_t)$ is the likelihood contribution of the demographic and behavioural data informing transition rates. Assuming independent vague priors for $\lambda_t$ and a Dirichlet(1, 1, 1, 1) prior for the compartment proportions at $t=1$, $c_1$, the joint posterior distribution for $c_1$ and $\lambda$, and therefore also of $\theta$, is obtained through MCMC implemented in WinBUGS. Note that the likelihood contribution of the prevalence data, $y_t$, depends on the $c_t$, the ODEs’ solutions, which are derived numerically for the current parameter values at each MCMC iteration using the Runge-Kutta algorithm in the WBDiff package in WinBUGS. Figure 4 shows posterior distributions resulting from the joint prevalence and incidence model.

5. DISCUSSION

From a methodological point of view, this work has responded formally to the need, perceived by epidemiologists working in the HIV arena, to “triangulate” all information: from multiple and imperfect sources and expert opinion on the epidemiological interpretation of the data from these sources. The approach is clearly appealing: it uses data fully, minimising potential biases due to selection of information; it typically leads to more precise estimates, which are consistent with all information; and it accounts for all sources of uncertainty, naturally reflected in the posterior distributions of parameters and quantities of interest.

5.2 Impact on the Real World

In principle, evidence synthesis does not need to be carried out in a Bayesian framework; see, for instance, Eddy, Hasselblad and Shachter (1992) and much of the meta-analytical work referenced in Sutton et al. (2000). Indeed, work exists to estimate HIV prevalence in a single risk group by synthesising three data sources in a classical approach, accounting for missing data (Walker et al., 2011). However, the unprecedented multiplicity of data sources, risk groups and indirect information involved in the work described here requires a Bayesian approach, with clear benefits over classical, likelihood-based alternatives. The main advantage is the ability to (i) explicitly introduce and (ii) formally quantify expert judgements. The hierarchical model introduced in Section 3.2 to tackle data sparseness offers such an example: only through reasonably chosen informative priors on the standard deviation hyperparameters has it been possible to overcome identifiability problems due to lack of information (see sensitivity analyses in Presanis, 2010). Second, a Bayesian model can be easily extended to include auxiliary “bias” parameters to quantify lack of validity and relevance of data items for the estimation for any specific parameter. Expert epidemiological information on the direction and magnitude of such biases is naturally accommodated in a Bayesian setup through carefully chosen priors (see Section 3.2 and references therein). It is not immediately obvious how a classical modelling approach would accommodate such information. Computational convenience represents a further advantage of a Bayesian approach. As the posterior distribution is estimated through simulation, it is straightforward to obtain inferences on any functional parameter of interest. The likelihood function of even a moderately sized evidence network is unlikely to be sufficiently tractable to allow comparably streamlined inference.
the official estimates of the magnitude of the HIV problem in the UK, in particular, the undiagnosed component, underlying current testing recommendations (http://www.hpa.org.uk/web/HPAweb&Page&HPAwebAutoListName/Page/1201094588821). In 2011, estimated trends on the prevalence of undiagnosed infection and incidence in MSM informed the work of the House of Lords Select Committee on HIV/AIDS in the UK (http://www.publications.parliament.uk/pa/ld201012/ldselect/ldaids/188/188.pdf). Recently, dissemination of the method has also attracted the interest of international public health organisations. Funded by the World Health Organization as part of an ongoing critical review of current methods for HIV prevalence estimation in concentrated epidemics (Ghys et al., 2008), the prevalence model has been adapted to estimate HIV burden in the Netherlands for the year 2007 (Conti et al., 2011). In comparison to other direct-type methods, the evidence synthesis approach was found to be the most flexible and statistically sound (van Veen et al., 2011).

5.3 Current Challenges

The model building and criticism processes in this work have led to a critical understanding of the strengths and weaknesses of the various sources of HIV information available in the UK, often challenging common interpretation of the data. Extensive sensitivity analyses have been carried out for prior and structural assumptions, to the sampling distributions employed, as well as to the data sources included (Goubar et al., 2008, Presanis et al. 2008, 2011, Presanis, 2010). Moreover, routine annual application of the model has led to continual model development, responding to changes in surveillance, the availability of new data sources, and ongoing model criticism in the cycle recommended by Box (1980) and O’Hagan (2003), amongst others. Some of the development required and in progress includes addressing issues of missing data, using ideas as in Walker et al. (2011) and a comprehensive model of the process of diagnosis in STI clinics based on a new surveillance system.
(http://www.hpa.org.uk/Topics/InfectiousDiseases/InfectionsAZ/HIV/OverallHIVPrevalence/).

More generally, model criticism is essential in an evidence synthesis approach. As data come from multiple sources depending on shared parameters, it becomes crucial to understand and communicate which sources (including priors) drive conclusions and whether the various items of evidence result in consistent or conflicting inference. Efforts clearly need to be focussed on the development of transparent methods for model assessment and criticism, given that evidence synthesis approaches are being increasingly employed in different areas of science.

In the same spirit, an important step toward improved communication and dissemination of Bayesian evidence synthesis would be the availability of a user-friendly computing environment, facilitating access and implementation of the methodology to nonexperts. van Veen et al. (2011) also identified the lack of such a modelling interface as a restriction to the more widespread adoption of our approach.

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