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Research Article

A Comparative Holistic Fuzzy Approach for Evaluation of the Chain Performance of Suppliers

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The competition between the companies in the dynamic market conditions has made the Supply Chain Management (SCM) a more important issue. The companies which have organized their supply chain effectively have obtained more flexibility in their manufacturing processes in addition to delivery of the customer demands. In this study, two different multicriteria decision making algorithms composed of the FAHP and a holistic hybrid method using FTOPSIS were utilized for an electronic company in wholly fuzzy processes. The FAHP is used for determination of the global weights of the factors and the performances of alternative suppliers are evaluated by using both FAHP-based and FAHP-FTOPSIS hybrid methods for synthetic extent values of pairwise comparisons. The sequences of the suppliers differed for the algorithms. The performances of the proposed approaches are quite successful and flexible in a narrow interval. The managerial advantages obtained from the proposed fuzzy algorithms are also analyzed and interpreted.

1. Introduction

The aim of a manager is to efficiently transport the products and services to the customer in a Supply Chain Management (SCM) system. Ensuring continuity and comparative degree for the administration is only possible by supplying and using the resources with high productivity, high quality, and low price. The administration has to realize flexible manufacturing and effective management for the supply chain from manufacturer to the final customer in order to compensate for the changing customer demand in a highly competitive environment.

In recent years, the integration of management functions within the borders of the administration is inadequate in terms of competition. Hence, the integration and effective management of activities beyond administration in the chain are quite necessary. Furthermore, the competition of supply chains has become much more important than the competition of the firms themselves. SCM is getting more important to accomplish this integration for fast and flexible covering of changeable customer necessities.

A supply chain can be described as a network used to supply necessary materials for manufacturing and service, to transform these to final products, and to transport the final products to the customers (e.g., suppliers, factories, warehouses, and distribution depots). A supply chain also offers different alternatives for distribution of products [1]. There exist a wide variety of definitions for SCM. For instance, Ellram [2] described the SCM as an integrated management approach which consists of planning and controlling material flow from supplier to customer. The experts of logistics see SCM as a management method for external flow of knowledge and inventory of the company.

Although SCM systems are quite important for the companies, enough importance is not given to the measurement and evaluation of performance of these processes. The existing research only focuses on the company's performance in market or the purchaser-seller relationship instead of the suppliers in whole system [3]. Holmberg's "cycle of supply chain measurement system improvement" model is the first research directly related to the improvement of a measurement system for interorganizations' supply chain

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performance [4]. The most common model for improvement approaches to performance measurement systems is the Balanced Score Card [5]. Brewer and Speh used this model for SCMs performance measurement systems [6]. Matthew and Miller worked on an improvement for a model with Activity Based Costing model [7]. Chan investigated the supply chain performance under qualitative and quantitative criteria [8]. Apart from the common criteria such as cost and quality, five other qualitative measurements are defined in the study such as resource utilisation, flexibility, visibility, trust, and innovativeness. Wei et al. presented a comprehensive framework with three main phrases to select an adequate SCM project that incorporates the strategies and operating routines of the supply chain [9]. Guneri et al. developed an integrated fuzzy and linear programming approach to the supplier selection problem [10]. Napalkova and Merkuryeva discussed two-phase optimization method based on hybrid combination of compromise programming, evolutionary computation, and response surface-based methods to balance optimal product demand and supply [11]. Chen et al. proposed a new integrated model by combining K-means clustering, feature selection, and the decision tree method into a single evaluation model to assess the performance of suppliers [12]. Che et al. developed a decision methodology for supply chain planning, taking into account such four criteria as cost, quality, delivery, and supplier relationship management and considering quantity discount and capacity constraints using analytic network process and turbo particle swarm optimization [13]. Rouyendegh and Erkan provided a guideline for establishing supplier selection criteria in respect to purchasing activities [14].

The evaluation of the performances of suppliers is the most important phase in SCM system. The phase can be described as a multicriteria decision problem regarding several factors in evaluation processes. The multi-criteria decision analysis (MCDA) for structuring these decision problems and evaluation of alternative suppliers provides a rich collection of methods. However, MCDA methods are often criticized because of their inability to handle the uncertain and imprecise problems. Thus, the fuzzy decision making was proposed as a powerful tool. Human has good ability in qualitative data processing which helps him/her to make decisions in fuzzy environment [15].

Fuzzy sets and fuzzy logic are powerful mathematical tools for modeling uncertain systems in industry, nature, and humanity and facilitators for common sense reasoning in decision making in the absence of complete and precise information [16]. Zadeh introduced the fuzzy set theory to deal with uncertainty due to imprecision and vagueness [17]. A major contribution of fuzzy set theory is its capability of representing vague data.

The fuzzy analytical hierarchy process (FAHP) and the fuzzy technique for order preference by similarity to ideal solution (FTOPSIS) methods are commonly used to address the multicriteria decision problems. The first study of FAHP is proposed by van Laarhoven and Pedrycz which compared fuzzy ratios described by triangular fuzzy numbers (TFNs) [18]. Buckley determines fuzzy priorities of comparison ratios whose membership functions trapezoidal [19]. Chang

introduces a new approach for handling FAHP with the use of TFNs for pairwise comparison scale of FAHP and the use of the extent analysis method for synthetic extent values of pairwise comparisons [20]. Cheng proposes a new algorithm for evaluating naval tactical missile systems by the FAHP based on grade value of membership function [21]. Zhu et al. discuss extent analysis method and applications of FAHP [22]. Kulak and Kahraman used this method for multicriteria selection among transportation companies [23]. Durán and Aguilo used FAHP for the evaluation and justification of an advanced manufacturing system [24]. Önüt et al. combined fuzzy multicriteria decision making approach for selecting shopping center site [25]. Deng et al. mentioned that existing methods of AHP cannot handle the uncertainties such as imprecision, fuzziness, and incompleteness [26]. However, Zhü discussed the validity of operational rules of fuzzy numbers and fuzzy sets theory for FAHP [27].

Chen and Hwang first applied fuzzy numbers to establish a prototype fuzzy technique for order preference by similarity to ideal solution (FTOPSIS) [28]. Chu and Lin suggested a FTOPSIS model, where rating of alternatives under criteria and importance weights of criteria were assessed in linguistic values represented by fuzzy numbers [29]. Rouyendegh proposed two intuitionistic aggregation operators in order to perform fuzzy group decision making for project selection [30]. Torfi et al. suggested a hybrid methodology with FAHP and FTOPSIS, which is the closest to this study [15].

As it is explained above, the evaluation of the supplier performance is one of the most important issues in management of supply chain. By using appropriate criteria and a systematic approach, the measurement of these performances is inevitable for the chain's success and competitive advantage. In this study, two types of algorithms have been suggested for evaluation of suppliers' performance and selection of the best possible supplier regarding its performance in one of the biggest electronic companies in Turkey. In this model, first, one of the techniques of fuzzy multicriteria decision making, that is, FAHP, is used to calculate global weights of the criteria and these weights are considered for both algorithms. Then, the FAHP-based performances and the rankings of FAHP-FTOPSIS hybrid algorithm are used to select the best alternative supplier, separately. In Section 2, the methodology of this study including basic concepts of fuzziness and fuzzy decision analysis is given. The proposed models are applied in wholly fuzzy processes with a numerical example for selected electronic company in Section 3. Finally, the research results and conclusion remarks are summarized in Section 4.

2. Methodology of Determination of Suppliers' Performances

A fuzzy set is a class of objects with a continuum of grades of membership. Such a set is characterized by a membership function, which assigns to each object a grade of membership ranging from zero to one.

In the following, some basic important definitions of fuzzy sets related to this study are given [31–35].

Definition 1. A fuzzy set \widetilde{M} in a universe of discourse X is characterized by a membership function $\mu_{\widetilde{M}}(x)$, which associates with each element x in X a real number in the interval [0,1]. The function value $\mu_{\widetilde{M}}(x)$ is termed the grade of membership of x in \widetilde{M} .

Definition 2. A TFN \widetilde{M} can be defined as a triplet (l, m, u), and the membership function $\mu_{\widetilde{M}}(x)$ is defined as

$$\mu_{\widetilde{M}}(x) = \begin{cases} 0, & x < 1, \ x > u \\ \frac{(x-l)}{(m-l)} & l \le x \le m \\ \frac{(u-x)}{(u-m)} & m \le x \le u, \end{cases}$$
 (1)

where l, m and u are real numbers and $l \le m \le u$. Algebraic operations with fuzzy number can be found in [35].

Definition 3. Let $\widetilde{M}_1 = (l_1, m_1, u_1)$ and $\widetilde{M}_2 = (l_2, m_2, u_2)$ be two triangular fuzzy numbers. Then, the distance between them can be calculated by using the vertex method as [32]

$$d\left(\widetilde{M}_{1},\widetilde{M}_{2}\right) = \sqrt{\frac{1}{3}\left[\left(l_{1}-l_{2}\right)^{2}+\left(m_{1}-m_{2}\right)^{2}+\left(u_{1}-u_{2}\right)^{2}\right]}.$$
(2)

Definition 4. A matrix \widetilde{D} is called a fuzzy matrix if at least one element is a fuzzy number [19].

The study proposes two types of algorithms for evaluating the performance of suppliers in the fuzzy MCDA. The steps of the proposed holistic method can be outlined as follows.

Step 1. Establish a fuzzy comparison matrix for each factor and criterion.

Let $X = \{x_1, x_2, ..., x_n\}$ be an object set and $U = \{g_1, g_2, ..., g_m\}$ a goal set. According to Chang's extent analysis, each object is taken and extent analysis for each goal g_i is performed, respectively. Therefore, m extent analysis values for each object can be obtained and shown as follows:

$$M_{g_i}^1, M_{g_i}^2, \dots, M_{g_i}^m, \quad i = 1, 2, \dots, n,$$
 (3)

where all the $M_{g_i}^j$ (j = 1, 2, ..., m) are TFNs.

Step 2. Calculate fuzzy synthetic extent with respect to the *i*th object which is defined as

$$S_{i} = \sum_{j=1}^{m} M_{g_{i}}^{j} \otimes \left[\sum_{i=1}^{n} \sum_{j=1}^{m} M_{g_{i}}^{j} \right]^{-1}.$$
 (4)

Note that \otimes denote the extended multiplication of two fuzzy numbers and

$$\left[\sum_{i=1}^{n}\sum_{j=1}^{m}M_{g_{i}}^{j}\right]^{-1} = \left(\left(\sum_{i=1}^{n}u_{i}\right)^{-1}, \left(\sum_{i=1}^{n}m_{i}\right)^{-1}, \left(\sum_{i=1}^{n}l_{i}\right)^{-1}\right).$$
(5)

The degree of possibility of $\widetilde{M}_2 = (l_2, m_2, u_2) \geq \widetilde{M}_1 = (l_1, m_1, u_1)$ is defined as $V(\widetilde{M}_2 \geq \widetilde{M}_1) = \sup[\min(\mu_{\widetilde{M}_1}(x), \mu_{\widetilde{M}_1}(y))]$ and can be equivalently expressed as follows:

$$V\left(\widetilde{M}_{2} \geq \widetilde{M}_{1}\right) = \operatorname{hgt}\left(\widetilde{M}_{1} \cap \widetilde{M}_{2}\right)$$

$$\mu_{\widetilde{M}_{2}(d)} = \begin{cases} 1, & m_{2} \ge m_{1} \\ 0, & l_{1} \ge u_{2} \\ \frac{l_{1} - u_{2}}{(m_{2} - u_{2}) - (m_{1} - l_{1})} & \text{otherwise,} \end{cases}$$
 (6)

where d is the ordinate of the highest intersection point D between $\mu_{\widetilde{M}_1}$ and $\mu_{\widetilde{M}_2}$. To compare \widetilde{M}_1 and \widetilde{M}_2 , we need both the values of $V(\widetilde{M}_1 \geq \widetilde{M}_2)$ and $V(\widetilde{M}_2 \geq \widetilde{M}_1)$.

The degree of possibility for a convex fuzzy number to be greater than k convex fuzzy numbers \widetilde{M}_i (i = 1, 2, ..., k) can be defined by

$$V\left(\widetilde{M} \ge \widetilde{M}_{1}, \widetilde{M}_{2}, \dots, \widetilde{M}_{k}\right)$$

$$= V\left[\left(\widetilde{M} \ge \widetilde{M}_{1}\right), \left(\widetilde{M} \ge \widetilde{M}_{2}\right), \dots, \left(\widetilde{M} \ge \widetilde{M}_{k}\right)\right] \quad (7)$$

$$= \min V\left(\widetilde{M} \ge \widetilde{M}_{i}\right), \quad i = 1, 2, \dots, k.$$

Assume that $d'(A_i) = \min V(S_i \ge S_k)$ for k = 1, 2, ..., n; k = i. Then the weight vector is given by $W' = (d'(A_1), d'(A_2), ..., d'(A_n))^T$, where A_i (i = 1, 2, ..., n) are n elements. Via normalization, the normalized weight vectors are

$$W = (d(A_1), d(A_2), ..., d(A_n))^T,$$
 (8)

where W is a nonfuzzy number [20, 36].

Step 3. Calculate the global weights, multiplying by normalized weights of factors and normalized weights of each criterion.

Step 4. Follow the following steps.

Step 4.1a. Choose the linguistic variables $(\tilde{x}_{ij} \ i = 1, 2, ..., n, j = 1, 2, ..., I)$ for alternatives with respect to criteria. The fuzzy linguistic rating (\tilde{x}_{ij}) preserves the property that the ranges of normalized triangular fuzzy numbers belong to [0, 1]; thus, there is no need for normalization (decisions of expert team).

Step 4.2a. Calculate the fuzzy performances points of alternative suppliers, multiplying the scale values and global weights.

Step 4.3a. Calculate the total fuzzy performance points for all suppliers and perform defuzzification.

Step 4.4a. Find the sequences of the performances of suppliers.

Step 4.1b. Use the same linguistic variables in Step 4a and establish the initial decision matrix for TOPSIS method.

Step 4.2b. Calculate the fuzzy weighted decision matrix by using global weights obtained by the FAHP.

Step 4.3b. Identify positive-ideal (A^*) and negative-ideal (A^-) solutions. The fuzzy positive-ideal (FPIS, A^*) and the fuzzy negative-ideal solution (FNIS, A^-) are shown as follows:

$$A^* = \{\widetilde{v}_1^*, \widetilde{v}_2^*, \dots, \widetilde{v}_i^*\}$$

$$= \{\left(\max v_{ij} \mid i \in I'\right) \times \left(\min v_{ij} \mid i \in I''\right)\},$$
where $I = 1, 2, \dots, J,$

$$A^* = \{\widetilde{v}_1^-, \widetilde{v}_2^-, \dots, \widetilde{v}_i^-\}$$

$$= \{\left(\min v_{ij} \mid i \in I'\right) \times \left(\max v_{ij} \mid i \in I''\right)\},$$
where $I = 1, 2, \dots, J,$

where I' is associated with benefit criteria and I'' is associated with cost criteria. FPIS can be given $\tilde{v}_i^* = (1,1,1)$ and $\tilde{v}_i^- = (0,0,0)$ for benefit criterion and FNIS can be given $\tilde{v}_i^* = (0,0,0)$ and $\tilde{v}_i^- = (1,1,1)$ for cost criterion.

Step 4.4b. Calculate the distance of each alternative from A^* and A^- using the following equations:

$$D_{j}^{*} = \sum_{j=1}^{n} d\left(\widetilde{v}_{ij}, \widetilde{v}_{i}^{*}\right) \quad j = 1, 2, \dots, J,$$

$$D_{j}^{-} = \sum_{j=1}^{n} d\left(\widetilde{v}_{ij}, \widetilde{v}_{i}^{-}\right) \quad j = 1, 2, \dots, J.$$

$$(10)$$

Calculate then the total distances by using vertex method given in (2).

Step 4.5b. Calculate similarities to ideal solution using

$$CC_j = \frac{D_j^-}{D_i^* + D_j^-} \quad j = 1, 2, \dots, J.$$
 (11)

Step 4.6b. Rank preference order. Choose an alternative with maximum CC_j^* or rank alternatives according to CC_j^* in descending order (holistic approach) [33].

Step 5. Compare the results obtained from both FAHP-based evaluation and FAHP-FTOPSIS hybrid approaches.

3. An Application of the Proposed Approaches in the Company

The proposed model is applied for four alternative suppliers of an electronic company which share very similar features. The company produced several types of electronic cards with more than 400 employees. It is one of the biggest electronic companies in the Middle East region which realizes a significant amount of exports to many countries. The aim of this application is to propose MCDA approach to evaluate the performance of the alternative suppliers of the company in the chain. Schematic diagram of the proposed algorithms is provided in Figure 1.

As it is given in Figure 1, the first model used the FAHP weights to evaluate the suppliers with performance scales of each criterion and the second model for the evaluation of performance is composed of hybrid method with FAHP and FTOPSIS, consisting of three main basic stages as follows:

- (1) establishing the decision team and identifying the factors (first level: main factors) and criteria (second level: subfactors) to be used in the model,
- (2) using FAHP method, calculating the local weights of the factors and criteria by using fuzzy pairwise comparison matrices, and calculating the global weights then,
- (3) evaluating the alternatives with FTOPSIS by using FAHP weights and determination of the final ranking.

The proposed models are applied to a real life problem in order to measure the performance of suppliers in the chain. This application created proprietary solutions for the electronic company. This company, which has one of the biggest annual sales turnovers, is working with approximately 50 inside or abroad suppliers and trying to manage this complex supply chain. The four of these suppliers selected have similar technical specifications to test the proposed approaches.

First, a team is established for the SCM performance evaluation system improvement and the company's related managers and academicians experienced in SCM are included in this team. Then, the factors and the criteria which will be used in the chain performance are determined and the strategic goals are used for the critical success of the company's necessities. In gathering this information, a simultaneous study is done with both department managers and workers of the alternative companies. The process factors are evaluated on the basis of sales/marketing, logistics, manufacturing, and finance according to the literature and company's features and necessities

After determining the factors and criteria, weighting of the factors has been calculated for which the FAHP technique is used. The pairwise comparison judgment matrices are formed for the factors comparison. The values were obtained from the consensus of entire team. These matrices are evaluated and the local weights of the factors and the criteria are calculated. The main factors and 14 criteria included factor groups are given in Figure 2.

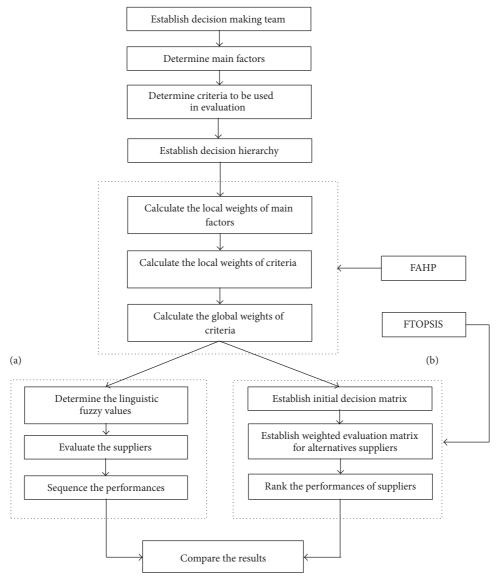
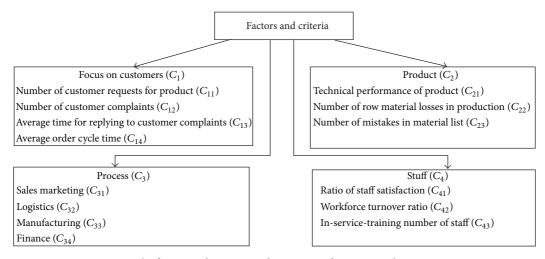


FIGURE 1: Schematic diagram of the proposed algorithms.



 $\label{thm:condition} \mbox{Figure 2: The factors and criteria used in SCM performance evaluating system.}$

TABLE 1: Linguistic variables for the important weight of each criterion.

Linguistic values	Triangular fuzzy numbers
Just equal	(1, 1, 1)
Equally important (EI)	(1/2, 1, 3/2)
Weakly more important (WMI)	(1, 3/2, 2)
Strongly more important (SMI)	(3/2, 2, 5/2)
Very strongly more important (VSMI)	(2, 5/2, 3)
Absolutely more important (AMI)	(5/2, 3, 7/2)

TABLE 2: Linguistic variables for the ratings.

Linguistic values	Triangular fuzzy numbers
Very low (VL)	(0, 0, 0.2)
Low (L)	(0, 0.2, 0.4)
Medium (M)	(0.2, 0.4, 0.6)
High (H)	(0.4, 0.6, 0.8)
Very high (VH)	(0.6, 0.8, 1)
Excellent (E)	(0.8, 1, 1)

TABLE 3: Pairwise comparison matrix of main factors.

	C_1	C_2	C_3	C_4
C_1	(1, 1, 1)	(3/2, 2, 5/2)	(1, 3/2, 2)	(2, 5/2, 3)
C_2	(2/5, 1/2, 2/3)	(1, 1, 1)	(1/2, 1, 3/2)	(1/2, 1, 3/2)
C_3	(1/2, 2/3, 1)	(2/3, 1, 2)	(1, 1, 1)	(1, 3/2, 2)
C_4	(1/3, 2/5, 1/2)	(2/3, 1, 2)	(1/2, 2/3, 1)	(1, 1, 1)

Initially, the fuzzy scale regarding relative importance to measure the relative weights in FAHP is given in Table 1. This scale is proposed by Kahraman et al. and used for solving several fuzzy decision making problems in the literature [37]. There are several scales available in the literature but this type of range is selected as consensual validation of the expert team. The linguistic variables for the problem are shown in Table 2. The same scale is also used for the hybrid method.

The fuzzy pairwise comparison matrix of the factors is stated in Table 3 and matrices of criteria are calculated in a similar way. The expert team is given the individual pairwise comparison matrix by using the scale given in Table 1. The all pairwise matrices are evaluated according to the consistency ratio and it is seen that all ratios are relevant in decision making (i.e., the inconsistency values are under 0,1).

The global weights of criteria used in the evaluation process are calculated using FAHP. The results obtained from the calculations based on the pairwise comparison matrices are presented in Table 4. In this table, the global weights are calculated, multiplying the weights and local weights.

The obtained global weights and determined linguistic variables are multiplied and the total performances are calculated. The results are defuzzified and the crisp performance values are obtained. The results of the algorithm at the end of the FAHP-based approach are shown in Table 5 and the sequences are given in Table 6. According to the table, the first performance in supply chain belongs to A_3 .

TABLE 4: Calculated global weights of the criteria with FAHP.

Factors	Weights	Criteria	Local weights	Global weights
-		(1.1)	0.226	0.101
Focus-on customers	0.447	(1.2)	0.189	0.084
(pcs/sec)	0.117	(1.3)	0.270	0.121
4		(1.4)	0.315	0.141
D 1 ((2.1)	0.501	0.081
Product (ratio/pcs)	0.161	(2.2)	0.248	0.040
(ratio/pes)		(2.3)	0.251	0.040
		(3.1)	0.315	0.080
Process	0.254	(3.2)	0.270	0.069
(pcs, \$)	0.231	(3.3)	0.189	0.048
		(3.4)	0.226	0.057
O		(4.1)	0.764	0.105
Stuff (ratio, pcs)	0.138	(4.2)	0.083	0.011
(ratio, pes)	1	(4.3)	0.153	0.021
			Total	1.000

Defuzzification formulation is given here as (l+4m+u)/6. Fuzzy initial decision matrix of TOPSIS method constructed for the evaluation of four suppliers (alternatives) of the electronic company by linguistic variables defined in Table 2 is presented in Table 7.

Using the global weights of criteria in Table 4, the weighted evaluation matrix is established by multiplying global weights and each column of initial FTOPSIS decision matrix and it is shown in Table 8. Here, the fuzzy positive and fuzzy negative ideal solutions are obtained.

The distance of each alternative from D^* and D^- can be currently calculated by using vertex method given by (2). The next step is to solve the similarities to an ideal solution by using (11). Then, the final results of FAHP-FTOPSIS hybrid approach are summarized in Table 9.

The positive and negative ideal solutions and also similarities to ideal solution are calculated. As shown in Table 9, the scales are very close to each other. The ranks of the suppliers are A_3 , A_1 , A_4 , and A_2 , respectively. The hybrid approach succeeds to rank very close alternatives.

In the last step, the results are compared and analyzed for both approaches. It is seen that A_3 is the best alternative supplier regarding chain performance for both methods but the sequences of the remaining performances of the suppliers are different although the methods used are the same global weights. In Table 10, the sequences and the performance values of two alternative evaluations are stated.

4. Conclusion and Discussion

In a competitive market, which has many suppliers dispersed in a wide geographical area with lots of opportunities for purchasing and distribution, beside the managerial activities of the companies makes it inevitable to high-dimensioned critical decision making for the managers. Furthermore, the

Criteria	Global weights	Linguistic performance value	Scale value	Fuzzy performance points
(1.1)	0.101	M	(0.2, 0.4, 0.6)	(0.020, 0.040, 0.061)
(1.2)	0.084	M	(0.2, 0.4, 0.6)	(0.017, 0.034, 0.051)
(1.3)	0.121	VL	(0, 0, 0.2)	(0, 0, 0.024)
(1.4)	0.141	Н	(0.4, 0.6, 0.8)	(0.056, 0.085, 0.113)
(2.1)	0.081	VL	(0, 0, 0.2)	(0, 0, 0.016)
(2.2)	0.040	M	(0.2, 0.4, 0.6)	(0.008, 0.016, 0.024)
(2.3)	0.040	VH	(0.6, 0.8, 1)	(0.024, 0.032, 0.040)
(3.1)	0.080	Н	(0.4, 0.6, 0.8)	(0.032, 0.048, 0.064)
(3.2)	0.069	Н	(0.4, 0.6, 0.8)	(0.027, 0.041, 0.055)
(3.3)	0.048	M	(0.2, 0.4, 0.6)	(0.010, 0.019, 0.029)
(3.4)	0.057	Н	(0.4, 0.6, 0.8)	(0.023, 0.034, 0.046)
(4.1)	0.105	VH	(0.6, 0.8, 1)	(0.063, 0.084, 0.105)
(4.2)	0.011	E	(0.8, 1, 1)	(0.009, 0.011, 0.011)
(4.3)	0.021	VH	(0.6, 0.8, 1)	(0.013, 0.017, 0.021)
Total points	1.000			(0.303, 0.463, 0.660)

TABLE 5: Fuzzy performance of Supplier #1 (A_1).

Table 6: Crisp values and sequences of the alternative suppliers' performances.

Alternatives	Total fuzzy points	Defuzzification	Rank
$\overline{A_1}$	(0.303, 0.463, 0.660)	0.469	4
A_2	(0.421, 0.621, 0.748)	0.609	2
A_3	(0.510, 0.710, 0.902)	0.709	1
A_4	(0.413, 0.613, 0.768)	0.606	3

efficiency in decision making depends on exact evaluation of performance of suppliers in time windows.

SCM and the process of the evaluation of supplier performance can be defined as MCDA problems for the companies. The conventional evaluation methods are inadequate in dealing with the imprecise or vague nature of linguistic assessments. To overcome this difficulty, fuzzy multicriteria methods are proposed in all steps.

Though the purpose of AHP is to capture the expert's knowledge, the conventional AHP cannot reflect the human thinking style. Therefore, FAHP and fuzzy extensions of AHP are developed to solve hierarchical fuzzy problems. This method has systematic approaches to alternative selection and problem justification by using the concepts of fuzzy theory and hierarchical structure analysis. Decision makers usually find that they are more confident to give interval judgments than fixed values judgments. This is because usually he/she is unable to explicit his/her preferences due to the fuzzy nature of the comparison process.

Using the FTOPSIS method, the decision maker's fuzzy assignments with different rating view points and tradeoffs among different criteria are considered in the aggregation procedure. to ensure more accurate decision making. This study uses TFN for both FAHP and FTOPSIS. The reason for using a TFN is that it is intuitively easy for the decision makers to use and calculate.

In this study, the evaluation of alternative suppliers' performance for a big electronic company is realized in wholly fuzzy processes. Firstly, the main factors and criteria for evaluation of the performance are determined by the expert team according to the company's necessities. The global weights of these criteria are calculated using FAHP technique. The supply chain performances of the alternative companies are evaluated using these weights and linguistic values of each supplier. The same weights are embedded in the FTOPSIS method and a hybrid algorithm is performed. In consideration of the results of the algorithms, the sequences differed. Regarding this difference, it is conceivable that the alternatives have very close technical features and/or the approximations of the methods into the problems are varied. The FTOPSIS method is substituted with the FAHP in most cases in the literature but there is no comparative degree with each other in the experiences up to now. In this manner, the proposed studies used in the application bring more flexibility to the company's performance evaluation

The first rank, that is, the best possible performance with the scale value of 0.445, belongs to Supplier A_3 . The scales of four alternatives are very close which range between 0.433 and 0.445. In such a narrow interval, the performance of the proposed hybrid algorithm is very successful and flexible. The algorithm serves a holistic approach for the performance evaluation system combined with both MCDA methods in the literature. Furthermore, it is suggested that the proposed flexible model could be easily used by the companies in different sectors, taking into consideration their own criteria in the SCM system.

As a future extension to this study, the relationships between the factors and criteria could be considered using Analytical Network Process (ANP), which is a powerful method. Hence, it is believed that both of the approaches could be used to obtain more accurate result in evaluating the chain performance.

	C_{11}	C_{12}		C_{42}	C_{43}
$\overline{A_1}$	(0.20, 0.40, 0.60)	(0.20, 0.40, 0.60)		(0.80, 1, 1)	(0.60, 0.80, 1)
A_2	(0.40, 0.60, 0.80)	(0.40, 0.60, 0.80)	• • •	(0.40, 0.60, 0.80)	(0.80, 1, 1)
A_3	(0.60, 0.80, 1)	(0.20, 0.40, 0.60)	• • •	(0.60, 0.80, 1)	(0.40, 0.60, 0.80)
A_4	(0.40, 0.60, 0.80)	(0.80, 1, 1)	• • •	(0, 0.20, 0.40)	(0.20, 0.40, 0.60)
Global weights	0.101	0.084		0.011	0.021

TABLE 7: Initial FTOPSIS decision matrix for four alternative companies.

TABLE 8: Weighted evaluation matrix for the alternatives.

	C_{11}	C_{12}	• • •	C_{42}	C_{43}
A_1	(0.02, 0.04, 0.06)	(0.02, 0.03, 0.05)	• • •	(0.01, 0.01, 0.01)	(0.01, 0.02, 0.02)
A_2	(0.04, 0.06, 0.08)	(0.03, 0.05, 0.07)	•••	(0.00, 0.01, 0.01)	(0.02, 0.02, 0.02)
A_3	(0.06, 0.08, 0.1)	(0.02, 0.03, 0.05)	•••	(0.01, 0.01, 0.01)	(0.01, 0.01, 0.02)
A_4	(0.04, 0.06, 0.08)	(0.07, 0.08, 0.08)	•••	(0.00, 0.00, 0.00)	(0.00, 0.01, 0.01)
A^*	$\widetilde{v}_{11}^* = (1,1,1)$	$\widetilde{v}_{12}^* = (0,0,0)$	• • •	$\tilde{v}_{42}^* = (0, 0, 0)$	$\tilde{v}_{43}^* = (0, 0, 0)$
A^{-}	$v_{11}^{-} = (0, 0, 0)$	$\tilde{v}_{12}^{-} = (1, 1, 1)$	•••	$\tilde{v}_{42}^{-} = (1, 1, 1)$	$\tilde{v}_{43}^{-} = (1, 1, 1)$

TABLE 9: FTOPSIS results of ideal solutions and ranking of alternatives.

Alternatives	D_j^*	D_j^-	CC_j	Rank
$\overline{A_1}$	3.656	2.896	0.442	2
A_2	3.657	2.794	0.433	4
A_3	3.524	2.821	0.445	1
A_4	3.625	2.820	0.438	3

TABLE 10: The comparison of both FAHP-based and FAHP-TOPSIS hybrid algorithms.

Alternatives	FAHP		Hybrid (FAHP-FTOPSIS)	
	Rank	Scales	Rank	Scales
A_1	4	0.469	2	0.442
A_2	2	0.609	4	0.433
A_3	1	0.709	1	0.445
A_4	3	0.606	3	0.438

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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