

# STATISTICAL SCIENCE

a review journal of the institute of mathematical statistics

**Volume 2**

**Number 1**

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## Featuring

**THE CALCULUS OF UNCERTAINTY IN  
ARTIFICIAL INTELLIGENCE AND EXPERT SYSTEMS**

**with articles by Glenn Shafer, Dennis V. Lindley,  
and David J. Spiegelhalter**

Joan Fisher Box on  
GUINNESS, GOSSET, AND FISHER

G. W. Stewart on  
COLLINEARITY AND LEAST  
SQUARES REGRESSION

**An Interview with C. R. RAO**

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