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***edited by***

**REINHOLD BAER**

**J. L. DOOB**

**A. H. TAUB**

**GEORGE W. WHITEHEAD**

**OSCAR ZARISKI**

# ILLINOIS JOURNAL OF MATHEMATICS

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## GEORGE ABRAM MILLER

Born in Lynville, Pennsylvania, in 1863; died in Urbana, Illinois, in 1951.

Bachelor of Arts (1887), Master of Arts (1890) from Muhlenburg College; Doctor of Philosophy (1892) from Cumberland University. Attended lectures of Lie in Leipzig and Jordan in Paris in the years 1895–1897.

Professor of Mathematics at Eureka College, 1888–1893;

Instructor, University of Michigan, 1893–1895;

Assistant Professor, Cornell University, 1897–1901;

Assistant and Associate Professor, Leland Stanford University, 1901–1906;

Associate Professor, Professor, and Professor Emeritus, University of Illinois, 1906–1951.

Elected to membership in the New York Mathematical Society in 1891; one of the organizers of the San Francisco Section of the American Mathematical Society in 1902, and Secretary of the Section until 1906; Chairman of the Chicago Section, 1907–1909; Vice-President of the Society, 1908. One of the founders of the Mathematical Association of America, 1915; Vice-President, 1916; President, 1921. Secretary of Section A of the American Association for the Advancement of Science, 1907–1912.

Member of the London Mathematical Society, Deutsche Mathematiker-Vereinigung, Sociedad Matematica Española; honorary life member of the Indian Mathematical Society, and of the Mathematical Association of America.

Fellow of the American Academy of Arts and Sciences; member of the National Academy of Sciences.

Doctor of Letters, Muhlenburg College.