

Amendments and Corrections

‘Time-scales for Gaussian approximation and its breakdown under a hierarchy of periodic spatial heterogeneities’

By R.N. Bhattacharya and F. Götze. *Bernoulli* (1995), 1, 81–123

There is an error in the estimates (4.45) of our paper. Because of the presence of the summand corresponding to $n = 0$, the correct estimates are

$$\begin{aligned} \sup_{x,y \in [0,a]^k} \dot{p}_a(1; x, y) z \leq c'' < \infty, \\ \sup_{x,y \in [0,1]^k} \ddot{p}^a(1/a^2; x, y) \leq c'' a^k. \end{aligned} \quad (1)$$

The main impact of this is that the time-scale $t \gg a^2$, or $t/a^2 \rightarrow \infty$, in Theorems 4.7, 4.9 and 4.10 should be replaced by

$$t \gg a^2 \log a \quad \left(\text{or } \frac{t}{a^2 \log a} \rightarrow \infty \right). \quad (2)$$

To see this, note that the rate of convergence to equilibrium as given in (4.48) and Lemma 4.2 is to be modified, in view of (1) above, to

$$\int_{[0,1]^k} |\dot{p}_a(t; x, y) - 1/dy| \leq c' a^k \exp\{-2\pi^2 \alpha t\} \quad (t > 0, x \in [0, 1]^k). \quad (3)$$

Equivalently, in Remark 4.1 a factor of a^k should be inserted in the right-hand side of the inequality, i.e.,

$$\int_{[0,a]^k} |\dot{p}_a(t; x, y) - a^{-k}/dy| \leq c' a^k \exp\{-2\pi^2 \alpha t/a^2\} \quad (t > 0, x \in [0, a]^k). \quad (4)$$

As a fairly immediate consequence of the modified estimate (3), one needs to insert a factor of a^k in the right-hand sides of inequalities (4.50)–(4.52) of Corollary 4.4. The remaining estimates (4.53)–(4.55) of Corollary 4.4 remain valid. To see this, use the obvious estimate

$$\| \tilde{T}_s f - \bar{f} \|_\infty \leq 2 \| f \|_\infty \quad \text{for } 0 \leq s \leq c \log a, \quad (5)$$

for an appropriate large constant c (not depending on a). For $s > c > \log a$, use the

modified version of (4.50), namely,

$$\| \tilde{T}sf - \tilde{f} \|_{\infty} \leq c_1 \|f\|_{\infty} a^k \exp\{-2\pi^2 \alpha t\}. \quad (6)$$

With these modified estimates, the proofs of Theorems 4.7, 4.9 and 4.10 carry over under the new time-scale (2).

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‘Branching processes as Population Dynamics’

By P. Jagers. *Bernoulli* (1995), 1, 191–200.

The formula on line 13, p. 195 of *Bernoulli*, 1, and the preceding sentence should read: The probability of an r -individual having a mother with type $\in ds$, who gave birth to that individual u time units ago, is

$$\pi(ds)e^{-\alpha u} \mu(s, dr \times du) / \pi(dr).$$

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