is a derivative; therefore* there exists on $[s_0 - \epsilon, s_0 + \epsilon]$ a set of positive measure for which $\phi(s) > 1 - \delta$, "..., which contradicts the theorem quoted above."

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A CORRECTION AND AN ADDITION

BY G. E. RAYNOR

- 1. A Correction. In a former paper† by the author the minus sign on the right side of equation (4), page 888, makes the notations of equations (4) and (5) for the function G inconsistent. This difficulty may be removed by changing the sign of G throughout the paper wherever the first argument of G has r_1 in the denominator. This change makes the first footnote on page 888 superfluous and it should be deleted. The second argument of G in equations (9) and (20) should be 0 instead of θ .
- 2. An Addition. The mean value of the function Φ over the circle C_2 was considered, in the paper, for the case of the singular point P outside of C_2 and for the case of P inside of C_2 . The question naturally arises as to what the situation is in case P lies on C_2 . This third case is not, however, of much interest since the integral

$$\int_{C_{\bullet}} \Phi ds,$$

which is now in general improper, will not in general exist. This may readily be verified for the function

$$\Phi = \left(\frac{r^2}{r_1^2} - \frac{r_1^2}{r^2}\right) \cos 2\theta$$

integrated over the circle C_2 , whose equation is $\rho = r_1 \sin \theta$. It will be found that even the principal value of the above integral is infinite while of course the value of Φ at the center of C_2 is finite.

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^{*} Hobson, Theory of Functions of a Real Variable, vol. 1, §403.

[†] On the extension of the Gauss mean-value theorem to circles in the neighborhood of isolated singular points of harmonic functions, this Bulletin, vol. 36 (1930), pp. 887-893.