# THE ANNALS of MATHEMATICAL STATISTICS

FOUNDED AND EDITED BY H. C. CARVER, 1930-1938 EDITED BY S. S. WILKS, 1938-1949

### THE OFFICIAL JOURNAL OF THE INSTITUTE OF MATHEMATICAL STATISTICS

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