

# A Conversation with Howell Tong

Kung-Sik Chan and Qiwei Yao

*Abstract.* Howell Tong has been an Emeritus Professor of Statistics at the London School of Economics since October 1, 2009. He was appointed to a lectureship at the University of Manchester Institute of Science and Technology shortly after he started his Master program in 1968. He received his Ph.D. in 1972 under the supervision of Maurice Priestley, thus making him an academic grandson of Maurice Bartlett. He stayed at UMIST until 1982, when he took up the Founding Chair of Statistics at the Chinese University of Hong Kong. In 1986, he returned to the UK, as the first Chinese to hold a Chair of Statistics in the history of the UK, by accepting the Chair at the University of Kent at Canterbury. He stayed there until 1997, when he went to the University of Hong Kong, first as a Distinguished Visiting Professor, and then as the Chair Professor of Statistics. At the University of Hong Kong, he served as a Pro-Vice-Chancellor and was the Founding Dean of the Graduate School. He was appointed to his Chair at the London School of Economics in 1999. He is a pioneer in the field of nonlinear time series analysis and has been a scientific leader both in Hong Kong and in the UK. His work on threshold models has had lasting influence both on theory and applications. He has drawn important connections between time series and deterministic dynamical systems, linking statistics with chaos theory, and the models he has developed have found significant applications in fields as diverse as economics, epidemiology and ecology. He has made novel contributions to nonparametric and semi-parametric statistics, especially in model selection and dimension reduction for time series data. He has written four books (one with Kung-Sik Chan and another with Bing Cheng) and over 162 papers (sometimes with collaborators) in Statistics, Ecology, Actuarial Science, Control Engineering, Reliability, Meteorology, Water Engineering, Engineering Mathematics and Mathematical Education. His 1990 monograph *Non-linear Time Series Analysis—A Dynamical System Approach* is a classic. He is a Foreign Member of the Norwegian Academy of Science and Letters, an elected member of the ISI, a Fellow of IMS and an Honorary Fellow of the Institute of Actuaries (UK). He won a Chinese National Natural Science Prize (Class II) in 2000 and the Royal Statistical Society awarded him the Guy Medal in Silver in 2007.

The following conversation is partly based on an interview that took place in the Hong Kong University of Science and Technology in July 2013.

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**QY:** You were supervised by Maurice Priestley for your doctorate. What was your thesis on?

**HT:** My doctoral thesis was entitled “Some problems in the spectral analysis of bivariate nonstationary stochastic processes.” It was an extension of Maurice Priestley’s evolutionary spectral analysis, which he proposed in 1965, from the univariate case to the bi-



FIG. 1. Howell with his childhood hero, Professor Loo Keng HUA, and Mary Tong, at Tong's home in Poynton, Cheshire, UK, 1979.

variate case, including both the open-loop and close-loop systems. The contents of the thesis formed the basis of a joint paper which Maurice and I read to the Royal Statistical Society in 1972. I can still remember the occasion well, as it was my first taste of academic subtlety in Britain.

I must tell you that a British statistician can do a clean demolition job at an RSS discussion meeting, without even showing his hammer. (I hope you will forgive me for being gender blind when I speak.) It has been said that one has to be courageous or foolhardy to read a paper to the RSS. I have learnt a lot besides the demolition skill since then, by attending RSS discussion meetings in London. The frankness of views is very helpful, as much for the readers as for the authors, because it enables everybody to have a more critical assessment of the strengths and weaknesses of the presented work. Of course, there will always be cases of premature euphoria as well as cases of misplaced cold shoulder. Despite its imperfection, I do not think that I am alone in saying that the forum remains the best in the statistical world. In many ways, it has made the RSS unique.

Returning to my doctoral thesis, I think much of it is now out of date and mostly of little practical significance. I am especially disappointed with the fact that the evolutionary coherency spectrum for nonstationary time series turns out to be time invariant. However, there is perhaps a curious little result in the thesis which you might find interesting. It concerns the function  $\exp\{i(k\omega t + \omega_0 t^2)\}$ ,  $\omega_0$  being a fixed constant. I showed that this frequency-modulated wave admits no generalized frequency in Priestley's sense. In

fact, I am inclined to take the view that for frequency-modulated waves the wavelet approach is more natural. In the 1990s, Bing Cheng and I developed a wavelet representation for a general stochastic process.

For the modelling of nonstationary time series, I think that the piecewise stationary approach introduced by Tohru Ozaki and myself in 1975 is a very practical one. Specifically, as each new "short" block of data arrives, we check if the AR model fitted to the latest block needs to be changed. If it does, then a new AR model is the latest state of the system, otherwise the previous state stays. This approach is ideally suited for real-time implementation. I understand that Professor Genshiro Kitagawa and his marine engineering colleagues have built many successful auto-pilots for boats based on this approach, under the guidance of the late Professor Akaike.

**QY:** Can you tell us something about the early part of your career in higher education?

**HT:** My first job in higher education was a lectureship at the then Northern Polytechnic, London, UK, in 1967. Remember I had only a B.Sc. degree! I took the job for two reasons: (1) To help my father financially because my mother had just joined us in London from Hong Kong, having waited for seven long years; (2) I lost my passion for Algebra.

When I graduated from the University of Manchester Institute of Science and Technology (now merged with the University of Manchester) in 1966, I was very keen on Algebra. So I went to Queen Mary College of the University of London on a postgraduate studentship funded by the UK Science and Engineering Research Council. The general expectation was to do a Ph.D. in Algebra.

At that time, QMC was the hot house of Algebra in the UK, under the inspiring leadership of Professor Kurt Hirsch. He came to the UK to escape from Hitler's Germany, like many of his contemporaries including Bernard Neumann, Hanna Neumann, Paul M. Cohn and others. He was my mentor. I remember attending courses on Homological Algebra, Group Representation Theory and others. I even attended seminars given by Saunders MacLane and other leading algebraists. One of the first things that Professor Hirsch asked me was "Have you studied Lebesgue integration at UMIST?" When he heard that I had not, he said, "In that case, Mr. Tong, you are only half-educated. I suggest that you attend a course on it in our inter-collegiate postgraduate programme."

As there was no dedicated Lebesgue Integration in that year's programme, I chose a course on Probability

Theory (via Measure Theory). The lecturer was none other than Professor Harry Reuter from Imperial College, London. Much later I learned that he was famous for his collaborative work with David Kendall on birth-and-death processes etc. Again, he, the son of the Socialist Mayor of Magdeburg, came as a young man to the UK to escape Hitler's Germany; he was looked after by the Cambridge mathematical analyst, Professor Charles Burkill, and his charitable wife, Greta Braun. Professor Reuter was such a wonderful lecturer that he got me hooked. In fact, his course made me reconsider my entire academic direction.

I decided that Probability would be far more fun and useful. The decision to quit Algebra was not painful. One must always follow one's passion. So, I can honestly claim that I was facilitated by a famous algebraist into Statistics. (In doing so, I dropped from the 13th generation of academic descendants of Sir Issac Newton to the 14th, according to the Mathematics Genealogy Project!) You see, I have had experiences of discontinuous decisions more than once in my life. Thresholds have been truly an integral part of my life in more senses than one.

As it turned out, I stayed at the Northern Polytechnic for just one year. My teaching duty was not heavy and I had free time to read around. I read several books on probability and stochastic processes. For example, I came across the delightful book on the theory of time series by Akiva Yaglom, which kindled my interest in the subject. Many years later, I was able to thank Akiva in person for his introduction. I met him in 1986 at the



FIG. 2. With Akiva Yaglom and his wife at the foot of the Tian Shan Mountain on the Tashkent side, 1986.

First Bernoulli World Congress held at Tashkent in the former USSR; we were both walking up the Heavenly Mountain (or Tianshan) from the Soviet side. We became instant friends. Do you know that the theoretical underpinnings of the ARIMA model made popular by George Box and Gwilym Jenkins were already laid rather fully by him in 1955? I learned this fact from Peter Whittle's charming book *Prediction and Regulation*, first published in 1963, when he was Professor of Statistics at Manchester. The book contains many gems and has remained one of my favourites since my days at the Northern Polytechnic. Another book that also captured my attention was the one by Ulf Grenander and Murray Rosenblatt entitled *Analysis of Stationary Time Series* (1957). You know, in my day there were not too many books on time series. One could probably count them on the fingers of one or two hands.

At the Northern Polytechnic, there was then a small study group on forecasting led by Dr. Warren Gilchrist, who later moved to head the Statistics Department at the Sheffield Polytechnic, now called the Sheffield Hallam University. I went along mainly to listen. Then one day I was asked if I would like to speak to the group on a paper of my choice. I happened to be studying Jim Durbin's *Biometrika* paper on the fitting of a moving average model via a long autoregression. I remember showing the group all my calculations, which helped me understand the paper and survive my first seminar. Little could I foresee at the time that my path would cross Durbin's several times later in my life. When Priestley's name was mentioned at one of the meetings of the study group, I looked up some of his papers, after which I knew that I would have to return to UMIST!

You see, Maurice came to UMIST just when I was starting my final undergraduate year; he lectured to us on mathematical statistics and stochastic processes. We at UMIST had excellent exposure to Statistics through Peter Wallington and Maurice Priestley. The former worked on queuing theory under Dennis Lindley. The only trouble was that they made the subject LOOK so easy that two of the more academically inclined students, including myself, opted for something more abstract like Algebra!

To cut a long story short, Maurice welcomed me back. In fact, thanks to an oversight on the part of the head of department (Maurice was not the Ho.D.), I was appointed as a demonstrator to compensate for the SERC postgraduate studentship that the Ho.D. forgot to apply on my behalf. The upshot was that I started my university teaching career as a postgraduate student and joined the university pension scheme at quite



FIG. 3. *Edinburgh Workshop on Nonlinear Time Series* Howell organised in 1989 (left to right ignoring row number: Wai-Keung Li, Ruey Tsay, Colin Sparrow, Russell Gerrard, John Lane, Murray Rosenblatt, Gudmundur Gudmundsson, John Petrucci, Tze-Liang Lai, Tony Lawrance, Peter Robinson, Dominic Guegan, T. K. Brown, Pham Dinh Tuan, Timo Terasvirta, Rodney Wolff, Clive Granger, Peter Fisk, David Cox, Martin Casdagli, Jonathan Tawn, Tohru Ozaki, Granville Tunnicliffe Wilson, Howell Tong, Dag Tjostheim, Ed McKenzie, Peter Lewis, Richard Smith, Neville Davies, David Jones, Kung-Sik Chan, Zhao-Guo Chen).

a young age. This turned out to be very beneficial many years later when my university pension (based on defined benefits) was calculated.

**QY:** What made you shift from frequency-domain to time-domain in your research in time series analysis?

**HT:** As we all know, the history of time series analysis switches to and fro between the time domain and

the frequency domain. I started my research from the frequency-domain end. I stayed with it for a few years. Then in 1973, Maurice, Subba Rao and I got a research grant, with which Professor Hirotugu Akaike of Japan was invited to visit us for six months. Hiro's visit marked the beginning of the end of my frequency-domain research. Let me elaborate.



FIG. 4. *ISI meeting in Paris, 1989*. Left to right: Maurice Priestley, Tata Subba Rao, Mary Tong, Anna Tong, Ritei Shibata, Haruku Shibata, Nancy Priestley, Howell Tong.



FIG. 5. *International Conference on Financial Statistics, Hong Kong, 1999.*

The first phase of Hiro's time series research had been almost exclusively frequency-domain. He was in fact an international figure in the area. Then he started his collaborative research in designing a feedback controller for a cement kiln. To his dismay, he discovered that in the presence of feedback, the frequency-domain approach was inadequate due to a serious bias problem associated with the estimation of the frequency-response function. His findings were recorded in the *Proceedings of Spectral Analysis of Time Series* edited by Bernard Harris in 1967. This impressive piece of work led to the invitation from UMIST.

His visit gave me ample opportunities to learn from his experiences. He was working on his fundamental state-space work at the time, which culminated in identifying a state as a basis vector of the predictor space of a second-order stationary multivariate time series. His vast knowledge impressed me deeply, so I decided to visit his institute in Tokyo, Japan. He was very supportive of my wish. In the event, I was awarded a Royal Society Japan Fellowship without any trouble. I guess that I could well have been the only applicant, as the fashion of the day in the UK was to go westwards. The six months I spent at Hiro's institute completed my (inverse) Fourier transform and I returned to the UK as a predominantly time-domain person. I have already related the transformation process in my obituary of

Professor Akaike published by both the Royal Statistical Society and the Institute of Mathematical Statistics. Therefore, I shall not repeat the account here, except to say that his personal mini-library played a vital role.

**KSC:** Your earlier works in time series analysis were all linear. What made you decide to switch to nonlinearity?

**HT:** Again it had to do with an RSS discussion meeting. On 18th May, 1977, I read a very short paper to the RSS, as one of three discussion papers. At the meeting, two features were highlighted, namely, time-irreversibility and limit cycles. I can remember the challenging problem posed by Dr. Granville Tunnicliffe Wilson: "Would we not prefer a model which in the absence of such (he meant random) disturbances would exhibit stable periodic deterministic behavior—a limit cycle?" I decided to take up the challenge.

Coincidentally, around the same time, the Swedish control engineer, Professor K. Aström, gave a seminar at UMIST. He described a bilinear control system, in which the output is not just a simple linear function of past (control) input and past output but also their cross products. For time series analysts, an obvious way to imitate this framework is by replacing the control input by a stochastic noise. (Of course, in doing so we are replacing a manipulated variable by an unobservable one!) I played around with this idea for a bit and even published something on it.



FIG. 6. Hirotsugu Akaike enjoying Howell's after-dinner speech at a conference honoring Akaike, Yokohama, 2003.

However, very quickly I convinced myself that was probably not the best way to address Granville's challenge: if I switch off the driving noise, the system would grind to a halt! One day, as I was mowing my lawn, strip by strip, it dawned on me that a piecewise linear model would be a good candidate. The rest is history, which you know I have recounted in the article "Birth of the threshold time series model" in *Statistica Sinica* (2007).

Actually, the earliest mention of the idea can be traced to my contribution to the discussion of Tony Lawrance and N. T. Kottegoda on modelling of riverflow time series in 1976. There was an interesting follow-up. At the time, it seems that my friend Tony could not see any relevance of the threshold idea to riverflow time series modelling. I am sure this was my fault. So, understandably he complained that I and one other contributor were "following a tradition of the Society in taking the opportunity to publicize their forthcoming works—at the expense of other authors' reprint charges." I hope that subsequent applications of the threshold model in riverflow time series modelling and linking of the Lawrance–Lewis's exponential autoregressive model to the threshold model have convinced him that the additional reprint charges were perhaps not unjustified.

**KSC:** Can you tell us more about the development of the threshold models, including their impact on ecology, economics and finance and other areas?

**HT:** I have given a fairly detailed overview in my article "Threshold models in time series analysis—30 years on" in *Statistics and Its Interface* (2011). I sincerely hope that the model will continue to enjoy its popularity with users from diverse disciplines. It makes



FIG. 7. Howell receiving the 2007 Guy Medal in Silver from President Tim Holt.

me a very happy man when I see applications of the model in econometrics, economics, finance, ecology, epidemiology, psychology, hydrology and many others. Frankly, some of the application areas are beyond my wildest dream. For example, just the other day my attention was drawn to cover song detection and bipolar disorder via the threshold model.

It would be wonderful if somebody could put all the most successful applications in book form. Hint, hint...

Now the basic idea of the threshold model is very simple: divide the state space into regimes and rule each with a simple linear model. It has a nonparametric flavor within a parametric framework. Of course, if we divide the state space arbitrarily finely, as in a spline approach, we gain generality at the expense of loss of parsimony or interpretability. Successful applications of the threshold model have shown that, in many real applications, two or three regimes will often suffice. Especially encouraging is the fact that quite often the regimes are interpretable. In mathematics, the idea of piecewise linearization is, of course, very old. In oscillations theory, the former Soviet mathematicians, Andronov and Khaikin, had introduced and studied (nearly) exhaustively piecewise linear differential equations in the 1930s. In statistics, we had two-phase linear regressions and Tukey's regressogram a long time ago, but it seems that they had made no or little impact on time series modelling, till the launching of the threshold autoregressive model and more generally the threshold principle. I must say that from the standpoint of stochastic dynamical systems, the incorporation of time in a regression framework is a

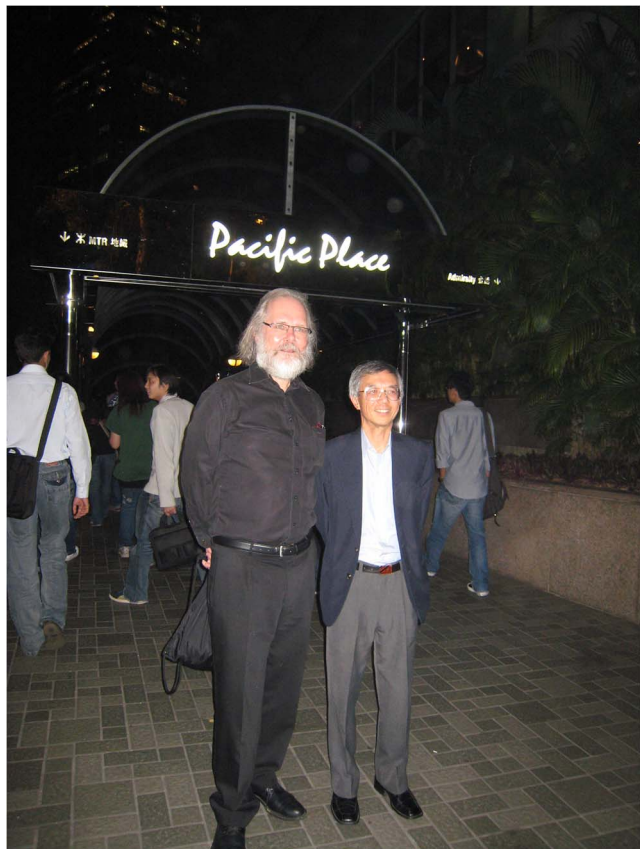


FIG. 8. Nils Christian Stenseth and Howell, in Hong Kong, 2008.

paradigm-shifting step because without time there is no dynamics. This is why I hail Yule's invention of the autoregressive model as one of the greatest revolutions in statistical modelling because it ushered in the era of dynamic (as against static) modelling. I find it unfortunate that some recent textbooks have blurred the distinction between a dynamic model and a static model.

Bruce Hansen (2011) has given an extensive review of the impact of the threshold model in econometrics and economics. Without any doubt, it is in econometrics/economics that the threshold model has made its greatest impact. More recently, the influence seems to be spilling into the field of finance including actuarial science.

Another significant area of application is ecology. Of course, you, Kung-Sik, have done some marvellous joint work with our dear friend, Nils Christian Stenseth of Norway. You have covered so much of the animal kingdom: mink, lynx, rodent, lemming and so on. Your more recent work with your former doctoral student, Noelle Samia, and Nils Christian's team on plague epidemics using data from Kazakhstan is truly wonderful. As your papers have shown yet again, often it is



FIG. 9. Mary, Peter Whittle and Howell, in Hong Kong, 2009.

through real applications that real progress on the implementation of what I have called the Threshold Principle can be made. You have implemented the principle for count data. I don't want to embarrass you, Kung-Sik, but I must say that the implementation is a truly remarkable contribution.

Of course, regimes can be delineated either sharply or smoothly. Coming from Hong Kong, I am rather happy with a sharp border! Well, the self-exciting threshold autoregressive (SETAR) model uses a sharp delineation. However, some people are less receptive to sharp delineations. In this case, we can consider a softer delineation, for example, a smooth (perhaps "soft" is a better word) threshold autoregressive model. You, Kung-Sik, and I have actually developed quite a comprehensive methodology and we have even given it the acronym of STAR model.

The idea has apparently attracted considerable attention in the econometrics literature, under the same acronym. I could perhaps make one or two remarks here. For simplicity, let us consider a one-threshold model. If the estimated threshold is in the vicinity of small probability, for example, near the tail or an anti-mode of the marginal distribution, then it tells us that there is probably insufficient information in the data on the functional form of the model there. In that case, whether we use an indicator function as in the SETAR model or a more sophisticated smooth function as in the STAR model is of secondary importance. After all, all models are wrong. When choosing between a SETAR model and a STAR model, a more relevant question is which one is more useful and interpretable.

More recently, you, Kung-Sik, Shiqing Ling, Dong Li and I have shown systematically how the threshold approach can provide powerful tools to model conditional heteroscedasticity in finance, environment, ecol-



FIG. 10. Qiwei Yao and Howell in Hong Kong, 2009, with Wai-Keung Li and Mike So in the background.

ogy and others. We have exploited the mixture of distributions in the driving noise of the threshold approach.

So far I have focused my answer on a univariate time series. Although there are generalizations of the threshold model to multivariate time series, I think much work remains to be done. One key question is the delineation of regimes for a  $p$ -dimensional state space. The topography can be quite vast. Too vast perhaps? My gut feelings are that it is still possible to construct an efficient search algorithm.

Besides the question of sharp and smooth delineation, there is also the one to do with observable or hidden threshold variables. I must tell you that I wasted an excellent research problem of Markov-chain driven TAR model in 1983 by assigning it to the wrong student; I should have passed it to you, Kung-Sik, and you would have cracked it in three months. The idea was there in the paper I read to the RSS in 1980 (page 285, line 12 from below).

Sometimes, we can even consider partially observable and partially hidden threshold variables. I have given a discussion in my 2011 recount in *Statistics & Its Interface*.

**KSC:** On looking back, the threshold idea is very natural. Nowadays the idea is applied in many areas, for example, ecology, economics and so on. And the TAR models are often featured very substantially in elementary text-books, for example, Walter Ender's *Applied Econometric Time Series Analysis* and Cryer and

Chan's *Time Series Analysis: With Applications in R*. Yet, the idea seems to have taken quite some time before it was universally accepted. Don't you think that this is a little odd?

**HT:** Well, it was probably my fault as much as yours for not being good salesmen! More seriously, as I have hinted at earlier, the history of statistics is full of cases of belated recognition as well as premature enthusiasm. Of course, there are also cases of instant recognition that have withstood the test of time. Like many other professions, value judgments by statisticians can sometimes be more subjective than scientific. I prefer to let TIME be the judge. I can remember Hiro Akaike saying to me many years ago (perhaps it was in the 1970s), "I reckon that AIC could probably survive 30 years." You see, even he had made the wrong prediction about his own baby!

**QY:** You have also had keen interest in chaos. How does chaos fit in with statistics in general and time series in particular?

**HT:** The primary object of study in Statistics is chance or, equivalently, randomness. The traditional view in statistics seems to place randomness at one end and determinism at the other. And it would be heresy to mix the two. In fact, every statistician carries with him  $\varepsilon$ 's everywhere, as if he owes his entire existence to them. If you ask him where his  $\varepsilon$ 's come from, he would give you a long list of sources, which is usually all right as far as it goes, except for the likely absence of one very significant ingredient. Let me digress first.





FIG. 11. P. S. Wong, C. K. Ing, N. H. Chan, W. Wu, K. L. Tsui, Peter Hall, T. L. Lai, R. Liu and Howell, at the Chinese University of Hong Kong, in 2009.

Suppose I toss a coin in this room. I hope you will agree that it is a reasonably close system free from external disturbances. Now, I can write down the precise equations of motion of the coin by appealing to Newtonian mechanics. But I also know I cannot predict its outcome with certainty, if I give it a good throw. Why? Where is the source of randomness? As long ago as the beginning of the 20th Century, H. Poincaré already included sensitivity to initial conditions as a significant source of randomness. So, even the most basic generator of randomness used by a statistician is a deterministic system; its randomness is due to what is called chaos by the dynamicists. Thus, what excuses can statisticians have to ignore chaos? Rather than burying our heads in the sand, I suggest that it is more constructive for us statisticians to learn more about chaos and make our contributions. Another interesting example is to do with point processes. Within the setup discussed in David Cox and Walter Smith (1954), we can identify a connection between point processes and chaos via the circle map:  $x_n = x_{n-1} + \Theta$ ,  $x_0 = 0$  ( $n = 1, 2, \dots$ ), where we observe  $y_n = x_n \bmod 1$ . Note that for irrational  $\Theta$ ,  $y$  is uniformly distributed on  $[0, 1)$ . I referred to this connection in my reply to David in my 1995 discussion paper in the *Scandinavian Journal of Statistics*.

You asked about time series. It turns out that many nonlinear time series models in statistics do generate chaos when we switch off the driving noise. That is what makes them so endearing! In a sense, there is

the inherent randomness due to chaos of the underlying deterministic system (I have called it the skeleton elsewhere), as well as the other randomness due to the random driving force, perhaps reflecting the fact that we are dealing with a complex system with multiple sources of randomness, some, but usually not all, of which can be explained with some degree of precision.

If we accept the above argument, then a natural question is how to define initial-value sensitivity of a *stochastic* dynamical system. Of course, Qiwei, you know the answer very well, as we have written about the topic. It turns out that the conventional approach adopted by the deterministic dynamicists is inadequate, as it ignores the diffusion due to the existence of multiple sources of randomness. Instead of looking at the movement of state  $x$  from one time instant to the next as they do in deterministic dynamics, we now look at the movement of one distribution  $F(x)$  from one time instant to the next. Since the focus is now on the distribution, we have to generalize the way we measure the sensitivity of the movement to initial values (i.e., initial distributions). We introduced a stochastic counterpart of the Lyapunov exponent. This experience shows the benefit of having statisticians involved in the study of deterministic chaos.

**KSC:** You interacted with people outside statistics. How did that come about?



FIG. 12. Howell with colleagues at the Nonlinear Time Series Workshop in National Singapore University, 2011; from left to right and ignoring rows: Dong Li, Qiwei Yao, Kung-Sik Chan, Mike So, Peter Brockwell, Ken Siu, Rainer Dahlhaus, Zudi Lu, Marc Hallin, Cheng Xiang, Richard Davis, Yingcun Xia, Ying Chen, Rong Chen, Howell Tong, Myung Seo, Shiqing Ling, Simone Giannerini, Cathy Chen, Azam Pirmoradian.

**HT:** Mostly by chance and more importantly by taking advantage of it. It is important to enjoy listening and have a sense of curiosity. For example, I collaborated with Dr. Gudmundsson of Iceland because I remembered that he was working on geophysical problems when he was a post-doctoral research fellow at UMIST. I met him there when I was a research student, and I listened to him and remembered what he had told me. So, many years later, I contacted him when I was interested in riverflow time series. Another example is Professor Nils Christian Stenseth. I met him via his doctoral student Ottar Bjørnstad, who contacted me and invited me to visit his department. I went to Oslo, listened to him and his colleagues and found the team there ideally placed for collaborative research. Nowadays, the internet is wonderfully convenient. Sometimes, I have not even ever met my co-authors in person.

**QY:** Besides time series analysis, you have also worked in other areas of statistics, for example, Markov chain modelling, reliability, dimension reduction. What motivated you?

**HT:** They were mostly my part-time activities for a bit of fun, except for dimension reduction, which was serious business. By about the mid-1990s, I knew I had to get into nonparametrics and semi-parametrics. But they were developing very rapidly. It was not easy for me to keep up, especially at a time when I was heavily involved with administration. Luckily, Bing Cheng and you, Qiwei, arrived in Canterbury, UK. I have learned so much from you. Thank you very much! As for dimension reduction, there is an interesting story behind it. As you know, the area actually laid outside my normal expertise in the 1990s. I was starting my sabbatical leave at the University of Hong Kong from the University of Kent, UK, initially for three years—I was lucky. I knew that Dr. Lixing Zhu of the department (now chair professor at Baptist University, Hong Kong) was an expert in semi-parametrics. So, I discussed dimension reduction with him. I was not impressed with the need in the literature to under-smooth the estimator of the nonparametric function. It might also be then or perhaps a little later when I questioned the efficacy of techniques such as the sliced inverse regression estimation for time series because time-irreversibility is



FIG. 13. *Howell and Murray Rosenblatt, after the former received the Distinguished Achievement Award from the International Chinese Statistical Association at the Joint Statistical Meeting at San Diego, USA, in July 2012.*

the rule in real time series. Lixing shared my concerns but was himself very busy with other research problems, so he mentioned the problem to one of Professor Wai-Keung Li's new research students, Yingcun Xia. Yingcun was an exceptionally bright student. To cut a long story short, his doctoral thesis formed the basis of a joint discussion paper on MAVE which I, on behalf of the four authors, read to the RSS in 2002. The trick was to estimate both the nonparametric part and the parametric part jointly. In this way under-smoothing is rendered unnecessary.

**KSC:** We all know that you have held senior administrative positions in five universities across two continents. Can you share your experience with us please? Perhaps you could begin with the Chinese University of Hong Kong.

**HT:** After working at UMIST for 14 years, I thought it was high time for me to return to my birth place, Hong Kong. There was a newly created Department of Statistics at CUHK around 1981 and a new chair of statistics was advertised, to which I applied successfully. The new department in 1982 consisted of 5 faculty members including myself, one senior lecturer and three lecturers. (CUHK followed the British system at that time.) There were also one assistant computer officer (that was you Kung-Sik), one secretary and one messenger boy. Although I was the founding chair professor, actually I did not appoint them; all the faculty members were transferred from the Department of Mathematics and all the lecturers were formerly students of the senior lecturer. Fortunately we got on very well indeed. Staff and graduate students

had regular dim-sum lunches at a local restaurant. We shared the cost, the seniors paying more, of course—a workable socialist system! The biggest challenge was actually curriculum design. We decided that our first year undergraduates should receive good groundings in the guiding principles of our subject rather than routine mathematical manipulations. I was voted to be the guinea pig. It was fun and I learnt a lot myself! Professor George Tiao was our external examiner (another British practice) and he was most helpful and supportive. He made plenty of constructive suggestions and gave us every encouragement. He has been maintaining excellent relationship with CUHK and many other tertiary institutions in Hong Kong ever since.

**KSC:** What made you decide to leave CUHK in 1986?

**HT:** My decision to leave CUHK had nothing to do with local politics of the time. I was quite happy at CUHK and my vice-chancellor (equivalent to a university president in the US) was very happy too with the development of my department and the department has remained in very good shape to this day. In fact, it all happened quite by chance when I was visiting Professor David Cox's department at Imperial College, London. One day, David told me that a chair was to be advertised by the University of Kent at Canterbury, UK. He suggested that I could have a go if I was interested in returning to the UK. Well, I do not know to this day why UKC decided to appoint me instead of any one of three other very strong candidates. As it turned out, the biggest challenge was how to manage a not so united mathematics department, consisting of pure mathematicians, applied mathematicians and statisticians. There were three sections, three budget holders and all in one department. A bit crazy! A year or two after my arrival, the vice-chancellor appointed me as the director of my department (directorship was by appointment then). When I became aware of the wish of the university to build up statistics and actuarial science by running down (pure and applied) mathematics, I reminded the vice-chancellor first the history of Thomas Becket and then my plan. As the director of my department, I could not possibly run down two sections to fatten up the third, especially when the latter was associated with me. However, I could build up statistics without harming mathematics by (i) taking advantage of the donation secured by my predecessor from the Black Horse financial group to build a solid base for actuarial science; (ii) taking over a major portion of the management science group which was being or about



FIG. 14. Howell with a group of post-graduate students at National University of Singapore, 2012.

to be re-organised; (iii) consolidating statistical consulting activities and service provision to Pfizer, whose UK base was nearby. By the time I stepped down as director in 1993, the statistics group (including actuarial science and the consulting arm) grew to more than 30 full-time staff working under one roof, possibly the biggest in the UK then. Our research rating also went up from 2 when I joined to 4 when I stepped down.

**QY:** Yes, I can remember those exciting days when I joined you in 1990. Then you went to Hong Kong in 1997. Can you take us through that period please?

**HT:** Again it was purely by chance that I went to Hong Kong, this time to the University of Hong Kong. You see, HKU had a new and very enterprising vice-chancellor, Professor Patrick Cheng. He was working very hard to turn HKU from a sleepy teaching-oriented university created in the colonial days to a research-vibrant modern university. He was investing huge resources in attracting people from all round the world to HKU by creating positions such as distinguished visiting professorships. A long-time fellow time series analyst, Dr. (now Chair Professor) Wai-Keung Li, seized the opportunity and was instrumental in getting me appointed. I arrived in HKU in 1997 on a 3-year sabbatical leave (without pay, of course) from UKC. At that time, UKC also had a new vice-chancellor, Professor Robin Sibson. It was he who granted me the leave.

**QY:** You were a visitor and yet you became the founding dean of their graduate school. How did that come about?

**HT:** Well, it was all due to my big mouth as usual. My perpetual problem! After my arrival at HKU, one morning Wai-Keung (who was HoD) said to me, “Howell, as you are a chair professor, I’d suggest that you attend our senate meeting this afternoon if you can spare the time. You see, I cannot go because I have some departmental matters to attend to. Anyway, it might be fun for you to see how we operate at HKU.” It turned out that the controversial item on the agenda was the establishment of a graduate school at HKU. The debate was getting really heated. It did not take me long to realize that many of those who opposed setting up a graduate school were professors who came from Britain ten or twenty years previously during the colonial days. You can tell from their accents! I could see that the vice-chancellor and his team were getting nowhere. At this point, I thought I had to say something. So, I said, “As somebody who has just arrived from Britain, I would like to inform senate members, especially those who left that country many years ago, that the concept of a graduate school, no doubt an American concept, is being adopted by a rapidly increasing number of universities in Britain. I feel that this is an irreversible trend world-wide.” After that, the debate subsided and the motion was carried. The following morning, the vice-chancellor rang me up. After thanking me for my intervention, he invited me to be the founding dean. The rest is history. My wife joked with me afterwards, saying “I thought you wanted to escape to Hong Kong in order to have peace and quiet.

See what you have done. Serves you right with your big mouth!” Well setting up a graduate school at HKU was challenging, because my first job was to persuade nine faculties to relinquish their power to the graduate school, abide by some common rules and regulations and to accept supervision by the Graduate School. I had two associate deans (Professors John Malpas and Anthony Yeh) and one senior administrator (Mrs. Yvonne Koo) from the registry to assist me—we called ourselves the gang of four. We literally set down all the rules and regulations, down to the way we handled reference letters. We always sent a thank-you letter to each referee enclosing a copy of his/her reference letter. This is a good way to uncover monkey business. In just a few years, we succeeded in improving our thesis completion rate (after constant monitoring of progress) and employability of our graduate students (we ran a small number of compulsory language-enhancing and skill-empowering courses).

**KSC:** And you also became a pro-vice-chancellor (equivalent to a vice-president in the US system)!

**HT:** Yes, I did serve as PVC to three VCs at HKU. My portfolio changed from one VC to the next and it included, at different times, research, administration and development. The names did not mean much because the dividing line was not sharp. My research portfolio did mean that I was in charge of the university’s all important submission of research output to the Hong Kong University and Polytechnic Grants Committee, who decides our budget. The work was tedious but it had to be done methodically and colleagues had to be handled delicately and with compassion. I remember visiting a number of departments and chatting to all the 60 or so heads of departments.

**KSC:** You have collaborated with many people, mostly younger than you, in research. Can you share your experience with us?

**HT:** I have always enjoyed young companies. They are without baggage, full of vitality and can think the unthinkable. My experience suggests to me that it is far easier sharing crazy ideas with the young than with the old. The old tends to react almost immediately by saying, “They are wrong” or “They are trivial.” But the young would say, “Oh, that is interesting. Let’s see!” I also think that it is the duty of every statistician to work, from time to time, with somebody younger than himself, for otherwise there is no hope for the profession.

**QY:** Now that you have retired from the London School of Economics, how do you occupy your time?

**HT:** Now that I have retired from the chair from which Professor Jim Durbin also retired, it seems that I am as busy as ever. The freedom from administration has given me more time to think (hopefully deeper), travel and try other things. (I did enjoy administration when I had to do it. You see, I saw no point in complaining and making myself miserable.) Now, with my wife suddenly becoming a qualified keep-fit instructor in her retirement, I have been persuaded to exercise more regularly than I used to. I also try to keep up with the statistical literature and continue doing some research. I am not displeased with some of the recent results I shared with young colleagues. As a matter of fact, Yingcun and I published a discussion paper in *Statistical Science* in 2011. We argue that, for dependent data, the MLE and its equivalents are not necessarily the most efficacious when we know that the model is wrong. For example, for a wrong time series model, conventional methods still typically rely on functionals of the one-step-ahead predictors. We have challenged them. More recently, Kung-Sik, Shiqing Ling, Dong Li and myself have just had our paper on conditionally heteroscedastic AR models with thresholds accepted by *Statistica Sinica*, to do with the threshold approach.

I have joined the University for the 3rd Age, through which I have participated in activities that I have never imagined I could do. For example, I enjoyed the course on book-binding. In fact, I have turned my copy of Peter Whittle’s charming little book *Prediction and Regulation* from a poorly produced paperback version into an acceptable hardback. Do you know that Peter is also a bookbinder? I discovered this fact when I showed him the finished product. Moreover, I am now able to indulge myself more in History, Literature and Philosophy. One regret is that I am not trilingual or better. I would love to be able to enjoy, for example, *War and Peace* in Russian. So much is often lost in translation. Just compare Witter Bynner’s translation (possibly the best available):

“... Though I have for my body no wings  
like those of the bright-coloured phoenix,  
Yet I feel the harmonious heart-beat of the  
Sacred Unicorn...”

with the famous original verse of Li Shangyin (ca. 813–858).

I have digressed!

To me, retirement is one LONG (I hope) sabbatical leave that has opened doors into many fascinating avenues. I recommend it!

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