

Introduction to the Special Issue: Bayes Then and Now

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The arrival of David Bellhouse’s autobiography of Sir Thomas Bayes at the *Statistical Science* editorial office triggered an idea that eventually became this issue. Although there is a distinct difference in the exact interpretation of “Bayes” in the two sections (as one refers to the man and the other to the subject), we thought that editorial privilege was in order.

While there is some uncertainty about the date of his birth, Thomas Bayes was born approximately 300 years ago, and, although the connection with this English mathematician of the 18th century is not entirely clear (see Stigler, 1983), a field of Statistics has taken his name by putting his theorem

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

at the center of its paradigm. After two centuries of developments and changes, Bayesian statistics is now a considerable force in the modeling of random phenomenon and the analysis of complex data. With this issue we celebrate the good health of Bayesian statistics and, more importantly, point out the directions of development of this self-contained theory of statistics.

One issue worth mentioning is that, in its recent evolution, the pressure of practitioners of statistics and users of Bayesian methodology has clearly modified the approach to Bayesian statistics toward a less dogmatic perspective and pushed forward a stronger unification. While a completely unified theory is clearly impossible, as discussed in the foundational paper of Phil Dawid, some important developments have occurred in the past years that explain why the Bayesian and the Fisher–Neyman–Pearson approaches to testing hypotheses differ so much, and how they could reconcile from a certain (sequential) perspective. This latter

point is illustrated by Susie Bayarri and Jim Berger. A similar trend can be observed for model choice and the incorporation of non-Bayesian criteria (such as Akaike’s) as shown by Ed George and co-authors, with his paper with Merlise Clyde focusing on the problem of variable selection and model averaging.

The evolution of the range of Bayesian inference is clearly visible in nonparametrics, which seemed to be a frequentist *chasse gardée* till recent years. As shown in the papers by both Peter Müller and Fernando Quintana, and by Stephen Walker, the Bayesian approach can provide a more than satisfactory answer to the problem of modeling datasets without parametric prior assumptions.

Besides numerous theoretical developments in the past thirty years, and, arguably, the fundamental logic inherent to Bayesian inference (the *inverse problem* of conditioning on the result and evaluating *causes* from *effects*), another reason for the remarkable rise in the use of Bayesian techniques is the explosion in computational power that occurred at the end of the 1980s with the appearance of MCMC techniques. While (then) powerful personal computers were already available at the end of the 1970s, the existing simulation or numerical techniques were not able to handle the high-dimensional models found in hierarchical Bayesian analysis beyond toy examples. (At that time, importance sampling was still in its infancy and naïve importance functions were unable to face the challenge.) The paper by Andrieu, Douce and Robert describes the sudden impact on Bayesian analysis offered by MCMC techniques, and stresses the complementary impact this had on simulation technology. For example, the papers by Mike Titterton and Michael Jordan are an illustration of the dissolving of the frontier between Statistics and Computer Science. Complex structures like neural networks and other graphical models, that were somehow on the “wrong” side of the barrier, were incorporated into Bayesian statistics. Both papers also incorporate descriptions of variational methods which, although quite natural from a model choice perspective, have not yet met full recognition in the statistical community.

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While the domain of Bayesian applications seems universal, as has been seen in the past ten years, we highlight two dominant ones, medical statistics and genomics, as these are fields where the impact of the combination of Bayesian analysis and MCMC technology is clearly unarguable. Both David Spiegelhalter and Don Berry describe the role of decision theoretic tools in the analysis of health institutions and clinical trials, while taking a rather different stand on the connections with frequentist evaluations. Since David Spiegelhalter is one of the originators of the main MCMC software, winBUGS, the computation issues are mostly eliminated from his paper. The paper by Shane Jensen et al. also highlights the immense benefits of a Bayesian approach for the discovery of motifs in genomics. (The first Bayesian genomic analysis, with an introduction

to the Gibbs sampler, was the pathbreaking paper in *Science* by Lawrence et al., 1993.)

So we lift a glass to wish Sir Thomas a Happy Birthday, and celebrate the current and continuing health of Bayesian statistics.

Christian P. Robert, Guest Editor
George Casella, Executive Editor

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