#### Institute of Mathematical Statistics LECTURE NOTES-MONOGRAPH SERIES

# **Approximate Computation** of Expectations

Charles Stein
Stanford University

Institute of Mathematical Statistics

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Shanti S. Gupta, Series Editor

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