and not, as is often thought¹, from the laws of negation which have not yet been stated. We shall see that these laws possess the same property and consequently preserve the duality, but they do not originate it; and duality would exist even if the idea of negation were not introduced. For instance, the equality (\$ 12)

ab + ac + bc = (a + b) (a + c) (b + c)

is its own reciprocal by duality, for its two members are transformed into each other by duality.

It is worth remarking that the law of duality is only applicable to primary propositions. We call [after BOOLE] those propositions *primary* which contain but one copula (< or =). We call those propositions *secondary* of which both members (connected by the copula < or =) are primary propositions, and so on. For instance, the principle of identity and the principle of simplification are primary propositions, while the principle of the syllogism and the principle of compositions.

15. Definition of Negation.—The introduction of the terms o and 1 makes it possible for us to define *negation*. This is a "uni-nary" operation which transforms a single term into another term called its *negative*.² The negative of a is called not-a and is written a'.³ Its formal definition implies the following postulate of existence⁴:

^I [BOOLE thus derives it (*Laws of Thought*, London 1854, Chap. III, Prop. IV).]

² [In French] the same word *negation* denotes both the operation and its result, which becomes equivocal. The result ought to be denoted by another word, like [the English] "negative". Some authors say, "supplementary" or "supplement", [e. g. BOOLE and HUNTINGTON]. Classical logic makes use of the term "contradictory" especially for propositions.

3 We adopt here the notation of MACCOLL; SCHRÖDER indicates not-*a* by a_{I} which prevents the use of indices and obliges us to express them as exponents. The notation a has the advantage of excluding neither indices nor exponents. The notation \bar{a} employed by many authors is inconvenient for typographical reasons. When the negative affects a proposition written in an explicit form (with a copula) it is applied to the copula (< or =) by a vertical bar (< or =). The accent can be considered as the indication of a vertical bar applied to letters.

4 [BOOLE follows Aristotle in usually calling the law of duality the