and consequently the second formula of the distributive law,

$$
(a+c)(b+c)=a b+c
$$

For

$$
(a+c)(b+c)=a b+a c+b c+c
$$

and, by the law of absorption,

$$
a c+b c+c=c .
$$

This second formula implies the inclusion cited above,

$$
(a+c)(b+c)<a b+c
$$

which thus is shown to be proved.
Corollary.-We have the equality

$$
a b+a c+b c=(a+b)(a+c)(b+c)
$$

for

$$
(a+b)(a+c)(b+c)=(a+b c)(b+c)=a b+a c+b c
$$

It will be noted that the two members of this equality differ only in having the signs of multiplication and addition transposed (compare $\$ 14$ ).
13. Definition of 0 and r.-We shall now define and introduce into the logical calculus two special terms which we shall designate by $\circ$ and by r , because of some formal analogies that they present with the zero and unity of arithmetic. These two terms are formally defined by the two following principles which affirm or postulate their existence.
(Ax. VI). There is a term o such that whatever value may be given to the term $x$, we have

$$
\circ<x
$$

(Ax. VII). There is a term I such that whatever value may be given to the term $x$, we have

$$
x<\mathrm{I} .
$$

It may be shown that each of the terms thus defined is - unique; that is to say, if a second term possesses the same property it is equal to (identical with) the first.

