Advanced Studies in Pure Mathematics 23, 1994 Spectral and Scattering Theory and Applications pp. 17–26

Asymptotics for the Painlevé II Equation: Announcement of Result

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Submitted in honor of Professor S.T. Kuroda, from whom we have learned so much

1. Introduction

In this paper we study the asymptotics of a class of solutions of the (homogeneous) Painlevé II (PII) equation

(1.1)
$$u_{xx} = 2u^2 + xu , \qquad x \in \mathbb{R} ,$$

as $x \to \pm \infty$. Following the work of Flaschka and Newell [FN] and Jimbo, Miwa and Ueno [JMU] the PII equation can be solved by means of a Riemann-Hilbert (RH) factorization problem as follows ([FA]; see also [IN]). Let $\Sigma^{(1)}$ denote the oriented contour consisting of six rays, $\Sigma^{(1)} = \bigcup_{k=1}^{6} \left\{ \Sigma_{j}^{(k)} = e^{i(k-1)\pi/3} \mathbb{R}_{+} \right\},$

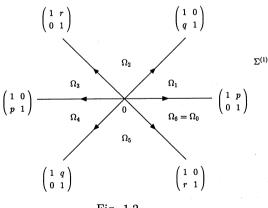


Fig. 1.2

Received February 8, 1993.