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The Geometry of Siegel Modular Varieties

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Introduction

Siegel modular varieties are interesting because they arise as moduli spaces for abelian varieties with a polarization and a level structure,