

Multiplicity One Theorems for Generalized Gelfand-Graev Representations of Semisimple Lie Groups and Whittaker Models for the Discrete Series

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Contents

§ 0. Introduction

Part I. Multiplicity one theorems for generalized Gelfand-Graev representations

§ 1. Generalized Gelfand-Graev representations (GGGRs)

§ 2. Sufficient conditions for multiplicity free property

§ 3. Spaces of Whittaker distributions

§ 4. Quasi-elementary Whittaker distributions on Bruhat cells

§ 5. Important types of GGGRs and their finite multiplicity property

§ 6. Multiplicity one theorems for reduced GGGRs

Part II. Whittaker models for the discrete series

§ 7. Irreducible highest weight representations and the holomorphic discrete series

§ 8. Method of highest weight vectors

§ 9. Preliminaries for determination of highest weight vectors

§ 10. Determination of highest weight vectors (Step I): Case of C^∞ -induced GGGRs

§ 11. Determination of highest weight vectors (Step II): Case of unitarily induced GGGRs

§ 12. Whittaker models for the holomorphic discrete series and irreducible highest weight representations

References

§ 0. Introduction

The idea of induced representation goes way back to G. Frobenius and I. Schur, and it has been always playing central and indispensable