

## Variation of Mixed Hodge Structure and the Torelli Problem

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*Dedicated to Professor Masayoshi Nagata  
on the occasion of his sixtieth birthday*

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