

Introduction to the Minimal Model Problem

Yujiro Kawamata, Katsumi Matsuda and Kenji Matsuki

Dedicated to Professor Nagayoshi Iwahori on his sixtieth birthday

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