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A FESTSCHRIFT IN HONOUR OF THE LATE GALAYE DIA
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***Hamet Seydi, Gane Samb Lo & Aboubakary
Diakhaby, Editors.***

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RELATED SCIENCES, A FESTSCHRIFT IN HONOUR OF
THE LATE GALAYE DIA**

Contents

Foreword to : A Collection of Papers in Mathematics and Related Sciences, a festschrift in honour of the late Galaye Dia	1
Chapter 1. Who was Galaye Dia (1941-2013)?, <i>by Profs Gane Samb Lo and Aboubakary Diakhaby</i>	5
1. Introduction	6
2. Scientific Career	6
3. Professional career	8
4. Services to the Mathematical Community	8
5. List of publications and supervision	9
Part 1. ALGEBRA	13
Chapter 2. A conjecture of Hartshorne, <i>by H. Seydi, T. H. Miabey and S. Maimouna.</i>	15
Bibliography	19
Chapter 3. Le théorème inverse de Galois, <i>by Hamet Seydi</i>	21
Bibliography	31
Chapter 4. Points algébriques de degré donné sur la courbe de Picard, <i>by Moussa FALL, Oumar SALL</i>	33
1. Introduction and motivations	34
2. Results and proofs	35
Bibliography	41
Part 2. STATISTICS AND DATA SCIENCES	43
Chapter 5. Sine-Skewed Cardioid Distribution, <i>by M. Ahsanullah</i>	45
1. Introduction	46
2. Main Results	47
Bibliography	55

Chapter 6. On the Parameter Estimation by the Moment Method and Wald Type Test for Poisson Processes, <i>by E. O. Accrachi, A. S. Dabye and A. A. Gounoung</i>	57
1. Introduction and motivations	58
2. Results and proofs	59
Bibliography	73
Chapter 7. Bidimensional Asymptotic Normality of the Moving Kernel Poverty Index Estimate, <i>by Y. Ciss and A. Diakhaby</i>	75
1. Introduction and definition of the estimator	76
2. Asymptotic Normality	78
3. Application	83
4. Details of the Proofs	83
Bibliography	111
Chapter 8. Adaptive kernel density estimation of income distribution and poverty index, <i>by Z. Baradine, Y. Ciss and A. Diakhaby</i>	113
1. Introduction and motivations	114
2. Convergence of the estimator	117
3. Simulations	120
4. Details of the Proofs	120
Bibliography	139
Chapter 9. Stochastic volatility model through MCEM: Departure from canonical SV model, <i>by M. M. Allaya and M. M. Kâ</i>	141
1. Introduction	142
2. Framework	142
3. Parameter estimation	143
4. Calibration to data	145
5. Departure from canonical sv model	152
6. Conclusion	158
Bibliography	161
Chapter 10. On the joint distribution of variations of the Gini index and Welfare indices, <i>by P. D. Mergane, G. S. Lo and T. A.Kpanzou</i>	163
1. Introduction and motivation	164
2. The asymptotic behavior of the Gini Index	176

3. Variation of the Gini Index between two dates	182
4. Mutual influence with the GPI	187
5. Final Comments	190
Bibliography	191
Chapter 11. Asymptotic Theory and Statistical Decomposability gap Estimation for Takayama's Index, <i>by M.C Haidara, T.A. Kpanzou, P.D. Mergane and G.S. Lo</i>	195
1. Introduction	196
2. The asymptotic behavior of Takayama's statistic	203
3. Statistical estimation of the default of decomposability	211
4. Data-driven applications	215
5. conclusion	218
Bibliography	219
Chapter 12. On some properties of the new Sine-skewed Cardioid Distribution, <i>by C.M.M Traoré, M. Diallo, G.S. Lo, M. Ahsanullah, L. C. Okereke</i>	221
1. Introduction	222
2. Asymptotic Properties of the tails	224
3. Parameters estimation	228
4. The characteristic function	230
5. Generation	232
6. Conclusion	233
Bibliography	243
Part 3. ANALYSIS AND GEOMETRY	245
Chapter 13. On the weak convergence in \mathbb{L}^p Spaces, <i>by Hamet Seydi</i>	247
Bibliography	255
Chapter 14. Computation of zeros of nonlinear monotone mappings in certain Banach spaces, <i>by T. M. Sow, M. Ndiaye, M. Sene and N. Djitte</i>	257
1. Introduction	258
2. Preliminaries	261
3. Main results	264
4. Application to convex minimization problems	268

5. Conclusion	270
Bibliography	271
Chapter 15. The $\partial\bar{\partial}$ -problem for extendable currents defined on a half space of \mathbb{C}^n , by <i>M. Eramane Bodian, W. Ndiaye and S. Sambou</i>	275
1. Introduction	276
2. Resolution of the equation $dS = T$ for a half space Ω of \mathbb{R}^{n+1}	277
3. Resolution of the $\partial\bar{\partial}$ for extendable currents in a half space of type $\{\text{Im}(z_n) < 0\} \subset \mathbb{C}^n$	279
Bibliography	281
Chapter 16. The Riemann extension of an affine Osserman connection on 3-dimensional manifold, by <i>A.S. Diallo</i>	283
1. Introduction	284
2. Preliminaries	284
3. Affine Osserman connections on 3-dimensional manifolds	288
4. Nonflat pseudo-Riemannian Osserman metric of signature $(3, 3)$	290
Bibliography	293
Chapter 17. Conformal transformation method for irrigation Dirichlet problem, by <i>F. Ndiaye, B.M. Ndiaye, M. Ndiaye, D. Seck and I. Ly</i>	295
1. Introduction	296
2. Preliminary	297
3. Identification of the domain by conformal mapping method	298
Bibliography	317
Part 4. PROBABILITY AND RANDOM ANALYSIS	319
Chapter 18. General Central Limit Theorems for Associated Sequences, by <i>H. Sangaré and G.S. Lo</i>	321
1. Introduction	322
2. A brief Reminder of Association	323
3. Central limit theorem for associated sequences	325
4. Results and Commentaries	329
Bibliography	341

Chapter 19. Homogenization of semilinear periodic parabolic PDEs with Reflecting boundary condition, <i>by A. Diedhiou, I. Sane, A. Coulibaly</i>	343
1. Introduction	344
2. Preliminaries	345
3. Main result	360
Bibliography	361
Chapter 20. On proximity between spectral elements associated with periodic and almost periodic stationary processes, <i>by E. N. Cabral</i>	363
1. Introduction	364
2. Notation and recalls	365
3. Spectral elements associated with periodic stationary process	371
4. Almost periodic stationary process	376
5. Periodic and almost periodic PCA in the frequency domain	379
6. Conclusion	384
Bibliography	385
Chapter 21. Strong limits related to the oscillation modulus of the empirical process based on the k-spacing process, <i>by G. S. Lo</i>	387
1. Introduction and statement of the results	388
2. Technical lemmas	394
3. Proofs of the results	403
Bibliography	411
Chapter 22. Gaussian Approximations and Related Questions for the Spacings process, <i>by G. S. Lo</i>	413
1. Introduction	414
2. The Gaussian approximation.	415
3. The Glivenko-Cantelli Theorem	427
4. The oscillation moduli	429
Bibliography	435
Chapter 23. A Simple Round-up on the Validity of a.s Convergence after Partial Modification of the Probability Law and Application, <i>by G.S. Lo</i>	437
1. Introduction and Motivation	438

2. General conditions for validity of types of limits after a marginal change of the sequence	440
3. Other sufficient conditions for conservation of the a.s. limits	443
4. Main Problem	447
5. Appendix	450
Bibliography	465
Part 5. MATHEMATICAL MODELLING	467
Chapter 24. Floquet theory and averaging methods : Useful tools for equilibrium stability of dynamical model of Typha proliferation, <i>by M. L. Diagne and T. Sari</i>	469
1. Introduction	470
2. Model	472
3. Floquet theory	474
4. Averaging method	478
5. Conclusion	482
Bibliography	485
Chapter 25. Numerical Solution of the 2-D Incompressible Non-stationary Navier-Stokes Equations by Adapted Projection Method, <i>by A.Seck, M. Ndiaye, A. Sy and D. Seck</i>	487
1. Introduction	488
2. About 2-D incompressible non-stationary Navier Stokes system	489
3. The proposed method: Projection method adapted to Navier-Stokes equations	495
4. Some concluding remarks and extensions	517
Bibliography	519
Chapter 26. Topological Optimization for Photonic and Phononic crystals problems, <i>by M.B. Dia, I. Faye and A. Sy</i>	523
1. Introduction and modeling	524
2. Modeling of crystal problems	525
3. Problem formulation and topological optimization	531
4. Application to photonics crystals problems and main result	534
5. Numerical simulations	542
Bibliography	557

Chapter 27. Numerical analysis of a corrector results in short term sand transport problem , <i>by B. K. Thiam, M. M. T. Baldé, I. Faye and D. Seck</i>	559
1. Introduction and results	560
2. Mathematical convergence and Homogenization	564
3. Two scale Numerical Method s	566
4. Numerical illustration	572
Bibliography	585
Chapter 28. Numerical simulations of sand transport problems, <i>by C. Diédhiou, B. K. Thiam and I. Faye</i>	587
1. Introduction and Results	588
2. Finite element method for Two scale limit	591
3. Numerical method for Reference model	596
4. Comparison Numerical Solution of Two-scale limit and reference solution	603
Bibliography	611
Part 6. CRYPTOGRAPHY AND NUMBER THEORY	613
Chapter 29. A note on Encoding and Hashing into Elliptic and Hyperelliptic Curves, <i>by N. Diarra, M. Seck and D. Sow</i>	615
1. Introduction	616
2. Preliminaries	618
3. Overview of (Hyper)Elliptic Curves Encoding	619
4. Overview of Hashing into (Hyper)Elliptic Curves	635
5. Unified Formulas for Hashing into (Hyper)Elliptic Curves	638
6. Conclusion	644
Bibliography	645
Part 7. GENERAL MATHEMATICS	649
Chapter 30. Réflexion sur la relativité de l'égalité mathématique à travers les notions de nombre, fonction, ensemble et l'affectation algorithmique, <i>by A. Maitournam</i>	651
1. Introduction	652
2. Egalité mathématique entre nombres	652
3. Egalité mathématique entre fonctions	653
4. Egalité mathématique entre ensembles	654

5. Egalité mathématique et algorithmique	654
6. Conclusion	655
Bibliography	657
Alphabetical Index	659