

LIST OF NOTATIONS

The meanings of letters and symbols will usually be clear from the context. In general, small Latin letters denote rational numbers, small Greek letters denote real or p-adic numbers, and capital Greek letters denote g-adic or g*-adic numbers. By Γ , P , P_p , P_g , and P_{g^*} we mean the fields of rational, real, and p-adic numbers, and the rings of g-adic, and g*-adic numbers, respectively. The symbols

$$|\alpha|, |\alpha_0|_p, |A|_g, \text{ and } |A^*|_{g^*}$$

stand for the absolute value of the real number α , the p-adic value of the p-adic number α_0 , the g-adic value of the g-adic number A , and the g*-adic value of the g*-adic number A^* , respectively.

Here $|\alpha_0|_p$ is normed by the formula

$$|p|_p = \frac{1}{p}.$$

The integer $g \geq 2$ always has the prime factorisation

$$g = p_1^{e_1} \cdots p_r^{e_r},$$

where p_1, \dots, p_r are distinct primes, and e_1, \dots, e_r are positive integers. If, for $j = 1, 2, \dots, r$, the g-adic number A has the p_j -adic component α_j , we write

$$A \leftrightarrow (\alpha_1, \dots, \alpha_r),$$

and then

$$|A|_g = \max \left(|\alpha_1|_{p_1}^{\frac{\log g}{e_1 \log p_1}}, \dots, |\alpha_r|_{p_r}^{\frac{\log g}{e_r \log p_r}} \right).$$

Thus, in particular,

$$|g|_g = \frac{1}{g}.$$

A g*-adic number A^* has, in addition to the p_j -adic components α_j , also a real component α . We write

$$A^* \leftrightarrow (\alpha, \alpha_1, \dots, \alpha_r) = (\alpha, A) \text{ where } A \leftrightarrow (\alpha_1, \dots, \alpha_r).$$

Then

$$|A^*|_{g^*} = \max (|\alpha|, |A|_g).$$

For rational integers $a, b, m \neq 0$ the congruence $a \equiv b \pmod{m}$ means, as usual, that $a - b$ is divisible by m . Instead of $a \equiv 0 \pmod{m}$ we write $m | a$. The symbol (a, b, \dots, f) means the greatest common divisor of the rational integers a, b, \dots, f , except on certain occasions when the same symbol is used to denote an ordered set of numbers. If α is a real number, $[\alpha]$ always denotes the integral part of α , i. e. the integer a for which $a \leq \alpha < a + 1$.

A formula like $a \in S$ means that a is an element of the set S . If S_1 and S_2 are sets, $S_1 \cup S_2$ is their union and $S_1 \cap S_2$ their intersection (i.e. $S_1 \cup S_2$ consists of all a that are elements of at least one of the sets, and $S_1 \cap S_2$ of all a that are elements of both sets.) The signs $\bigcup_k S_k$ and $\bigcap_k S_k$ are used for the union and intersection of any number of sets.