

whence we derive this practical rule: To obtain the resultant of the elimination of  $x$  in this case, it is sufficient to equate to zero the product of the coefficients of  $x$  and  $x'$ , and add to them the term independent of  $x$ .

**32. The Case of Indetermination.**—Just as the resultant

$$ab = 0$$

corresponds to the case when the equation is possible, so the equality

$$a + b = 0$$

corresponds to the case of *absolute indetermination*. For in this case the equation both of whose coefficients are zero ( $a = 0$ ), ( $b = 0$ ), is reduced to an identity ( $0 = 0$ ), and therefore is "identically" verified, whatever the value of  $x$  may be; it does not determine the value of  $x$  at all, since the double inclusion

$$b < x < a'$$

then becomes

$$0 < x < 1,$$

which does not limit in any way the variability of  $x$ . In this case we say that the equation is *indeterminate*.

We shall reach the same conclusion if we observe that  $(a + b)$  is the superior limit of the function  $ax + bx'$  and that, if this limit is 0, the function is necessarily zero for all values of  $x$ ,

$$(ax + bx' < a + b) (a + b = 0) < (ax + bx' = 0).$$

*Special Case.*—When the equation contains a term independent of  $x$ ,

$$ax + bx' + c = 0,$$

the condition of absolute indetermination takes the form

$$a + b + c = 0.$$

For

$$\begin{aligned} ax + bx' + c &= (a + c)x + (b + c)x', \\ (a + c) + (b + c) &= a + b + c = 0. \end{aligned}$$