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$$\begin{split} \Sigma_n & (\text{degree}) (\text{see } \Phi (\text{degree})) \\ \Sigma_n & (\text{formula, sentence}) \\ & (\text{see } \Gamma (\text{formula, sentence})) \\ \Sigma_1 &- \text{complete } 14 \\ \Sigma_n &- \text{conservative} \\ & (\text{see } \Gamma &- \text{conservative}) \\ \Sigma_1 &- \text{extension } 97 \\ \Sigma_1 &- \text{extension } 97 \\ \Sigma_n &- \text{sound } (\text{see } \Gamma &- \text{sound}) \\ & \text{self-prover } 71 \\ & \text{Shepherdson-Smorynski fixed} \\ & \text{point theorem } 51 \end{split}$$

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