# THE ANNALS of STATISTICS

## AN OFFICIAL JOURNAL OF THE INSTITUTE OF MATHEMATICAL STATISTICS

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The classification numbers representing the primary and secondary subjects of the article may be found with instructions for its use, as an Appendix to Mathematical Reviews Index to Volume 39, June 1970. (See, also, The Notices of the American Mathematical Society, June 1970, pp. 616-618, for more details.) The key words and phrases should describe the subject matter of the article; generally they should be taken from the body of the paper.

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