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Contents

	PAGE
On the comparison of two empirical distribution functionsLajos Tákacs	1157
Factorial association schemes with applications to the construction of multidimensional partially balanced designsJ. N. Srivastava and D. Á. Anderson	1167
A note on the existence of quantitative probability	1182
Confidence intervals for linear functions of the normal mean and variance $$\operatorname{\textbf{Charles}}$\ E.\ Land$	1187
Non-local asymptotic optimality of appropriate likelihood ratio tests. L. D. Brown	1206
The Bernstein-von Mises theorem for Markov processes J. Borwanker, G. Kallianpur and B. L. S. Prakasa Rao	1241
Noncentral distribution of Wilks' statistic in MANOVAA. K. GUPTA	1254
The topology of distinguishabilityLLOYD FISHER AND JOHN W. VAN NESS	1262
Model building for prediction in regression based upon repeated significance tests W. J. Kennedy and T. A. Bancroft	1273
On weak convergence of stochastic processes with multidimensional time parameter $$\operatorname{\textbf{Georg}}$$ Neuhaus	1285
Some asymptotic results in a model of population growth, II. Positive recurrent chains ${\bf Burton}$ Singer	1296
Partially balanced weighing designs with two association classes $\mathbf{K}.\ \mathbf{V}.\ \mathbf{Suryanarayana}$	1316
A characterization of invariant loss functions	1322
Nonparametric estimate of regression coefficientsJana Jureckova	1328
Sequential discrimination with likelihood ratios	1339
On the asymptotic optimality of spectral analysis for testing hypotheses about time series	1348
On a class of bivariate distributions following a certain stochastic structure Chandan K. Mustafi	1359
The equivalence of functional central limit theorems for counting processes and associated partial sums	1372
Formal Bayes estimation with application to a random effects model STEPHEN PORTNOY	1379
On fixed-width confidence bounds for regression parametersM. S. Srivastava	1403
On obtaining large-sample tests from asymptotically normal estimators ${f T}.$ ${f W}.$ ${f F}.$ Stroud	1412
Continued on back	cover

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	Blacksburg, Virginia (Eastern Regional)	Spring 1972		$\mathbf{A}\mathbf{S}\mathbf{A}$
	Ames, Iowa (Central Regional)	Spring 1972		ASA, ENAR
	Seattle, Washington (Western Regional)	Spring 1972		
	Ithaca, New York (Eastern Regional)	Spring 1973		ASA, ENAR
	Albuquerque, New Mexico (Western Regional)	Spring 1973		

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