THE ANNALS **APPLIED PROBABILITY**

AN OFFICIAL JOURNAL OF THE Institute of Mathematical Statistics

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