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HYPERBOLIC MANIFOLDS**

Hiroshi ISOZAKI

Yaroslav KURYLEV

INSTITUTE OF MATHEMATICS, UNIVERSITY OF TSUKUBA, TSUKUBA, 305-  
8571, JAPAN

*E-mail address:* `isozakih@math.tsukuba.ac.jp`

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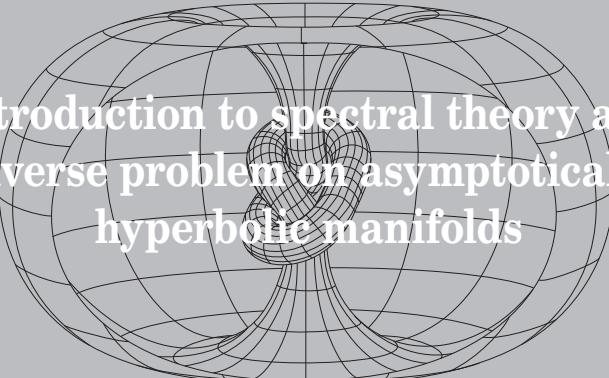
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Hiroshi ISOZAKI and Yaroslav KURYLEV



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Hiroshi ISOZAKI  
Professor  
Institute of Mathematics  
University of Tsukuba  
Tsukuba, 305-8571, Japan  
E-mail:isozakih@math.tsukuba.ac.jp

Yaroslav KURYLEV  
Professor  
Department of Mathematics  
University College London  
United Kingdom  
E-mail:y.kurylev@ucl.ac.uk

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