



Figure 8.1: Invariants of 3-manifolds and the relations between them

invariant for the perturbative invariants; see Figure 8.1 for relations between these invariants. In the figure we also show the present attainments.

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