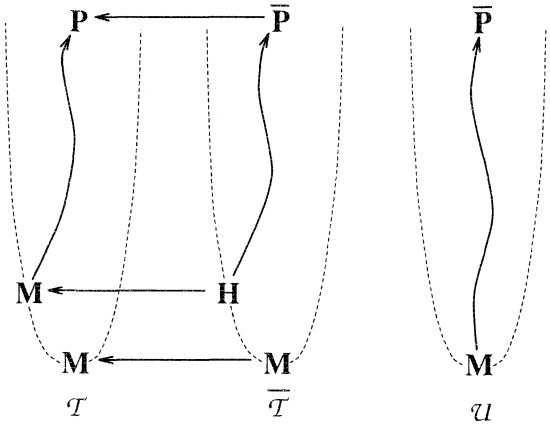
Lecture Notes in Logic 3

William J. Mitchell John R. Steel

Fine Structure and Iteration Trees



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Lecture Notes in Logic 3

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Springer-Verlag
Berlin Heidelberg New York
London Paris Tokyo
Hong Kong Barcelona
Budapest

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Mathematics Subject Classification (1991): 03E45, 03E55, 03E10, 04A10, 04A15

ISBN 3-540-57494-8 Springer-Verlag Berlin Heidelberg New York
ISBN 0-387-57494-8 Springer-Verlag New York Berlin Heidelberg

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Printed in Germany

SPIN: 10061642 46/3140-543210 - Printed on acid-free paper

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