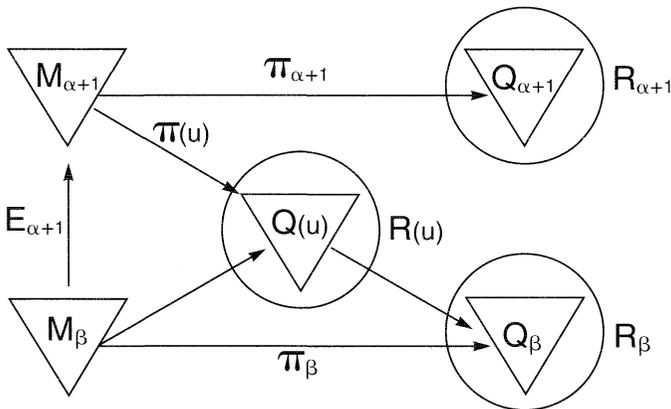


# Lecture Notes in Logic

8

John R. Steel

## The Core Model Iterability Problem



Springer

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# The Core Model Iterability Problem



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