Current Developments in Mathematics 2009

Edited by

David Jerison Barry Mazur Tomasz Mrowka Wilfried Schmid Richard Stanley Shing-Tung Yau



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