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Correction: ***Semi cubical theory on homotopy classification***
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p. 44. l. 1b. Insert sentences. "The *tensor product* $K\otimes L$ is an S.Q. complex defined as follows (See D. Kan: Abstruct Homotopy I, Proc. Nat. Acad. Sci. U.S.A. 41, 1092-1096):

$(K\otimes L)_{p+q}\ni(a_p, b_q)$ $a_p\in K$, $b_q\in L$, where $(D_{p+1}a_p, b_q)$ and (a_p, D_1b_q) are identified; the element represented by (a_p, b_q) is denoted by $a_p\otimes b_q$;

$$F_i(a_p\otimes b_q)=F_i(a_p)\otimes b_q \quad i\leqq p, \quad D_i(a_p\otimes b_q)=D_i(a_p)\otimes b_q \quad i\leqq p,$$
$$=a_p\otimes F_{i-p}(b_q) \quad i>p, \qquad =a_p\otimes D_{i-p}(b_q) \quad i>p."$$

p. 52. Insert sentences in the bigining of §7. "Two S.Q. maps T_0, $T_1: K\to L$ are called *S.Q. homotopic* if there exists a S.Q. map $F_I: Q(I)\otimes K\to L$ such that $F_I(\varepsilon_1^i\otimes\sigma)=T_i(\sigma)$ $i=0, 1$ for every cube σ of K (notation $T_0\cong T_1$). Two S.Q. maps T_0, T_1 are called *weakly S.Q. homotopic* (W.S.Q. homotopic $T_0\simeq T_1$) if there exists a sequence $T^{(0)}, T^{(1)}, \cdots, T^{(p)}$ such that $T^{(0)}=T_0$, $T^{(p)}=T_1$ and $T^{(i)}\cong T^{(i+1)}$ $i=0, \cdots, p-1$. This relation is an equivalence relation. The classes of S.Q. maps which are W.S.Q. homotopic are called *S.Q. homotopy classes*. We shall denote $Q(I)\otimes K$ by $I\otimes K$ in the follwing." Read "S.Q. homotopy" for "chain homotopy" in l. 11b, 10b. Insert between l. 2b-1b "$\bar\omega(\eta_1\cdots\eta_{p-1}\otimes\sigma_{n-p})=(-1)^{p-1}\omega(D_1^{p-1}\sigma_{n-p})$, where $D^m\sigma=D_1(D_1^{m-1})$."

p. 53. Insert between l. 4-5 "$\delta\bar\omega(\eta_1\cdots\overset{i}{\vee}\cdots\eta_p\otimes\sigma_{n+1-p})=(-1)^i\bar\omega[(\varepsilon_1^0\eta_1\cdots\eta_{p-1}-\varepsilon_1^1\eta_1\cdots\eta_{p-1})\otimes\sigma_{n+1-p}]+(-1)^p\bar\omega(\eta_1\cdots\overset{i}{\vee}\cdots\eta_p\otimes\partial\sigma_{n+1-p})=(-1)^{i+1}\delta\omega(D_1^{p-1}\sigma_{n+1-p})+(-1)^p\bar\omega(\eta_1\cdots\eta_{i-1}\otimes D_1^{p-i}\partial\sigma_{n+1-p})=(-1)^{i+1}\omega(\partial D_1^{p-1}\sigma_{n+1-p})+(-1)^{p+i-1}\omega(D_1^{i-1}D_1^{p-i}\partial\sigma_{n+1-p})=0$ since $\partial D_1=-D_1\partial$." Read "S.Q. homotopy" to "chain homotopy" in l. 9.

p. 54. Read "Proposition (7.3)" for "Lemma (7.3)", "Namely" for "Proof" and "S.Q. homotopy" in l. 3, 4, 5. Insert between l. 12b-11b "$y_q(\eta_1\cdots\eta_{p-1}\otimes\sigma_{n-p})=(-1)^{p-1}b_n(D(D_1^{p-1}\sigma_{n-p}))$ for $\sigma_{n-p}\in K_{n-p}$" and between l. 6b-5b "$y_q(\eta_1\cdots\cdots\eta_{p-1}\otimes\sigma_{q-p})=(-1)^{p-1}b_q(D(D_1^{p-1}\sigma_{q-p}))$ for $\sigma_{q-p}\in K_{q-p}$."

p. 55. Insert between l. 9-10 "$y_{q(i)}(\eta_1\cdots\eta_{p-1}\otimes\sigma_{q(i)-p})=(-1)^{p-1}b_{q(i)}(D(D_1^{p-1}\sigma_{q(i)-p}))$ for $\sigma_{q(i)-p}\in K_{q(i)-p}$." Read "S.Q. homotopy" for "chain homotopy" in l. 3b. Replace "$T(x_n)\cong T(x_n')$" l. 8b by "$T(x_n)\simeq T(x_n')$".

p. 56. Read "S.Q. homotopy" for "chain homotopy" in l. 15, "W.S.Q. homotopy" for "chain homotopy" in l. 13b, 10b, 5b. Replace "$T(x_n) \cong T(x'_n)$" in l. 11b, 5b by "$T(x_n) \simeq T(x'_n)$".

p. 57. Read "S.Q. homotopy" for "chain homotopy" in l. 2, 4b. Insert between l. 7-8 "$\bar{x}'_q(\eta_1 \cdots \eta_{p-1} \otimes \sigma_{q-p}) = 0$ for $\sigma_{q-p} \in K_{q-p}$."

p. 58. Replace the notation "$\cong$" l. 6, 9, 9b by "$\simeq$". Read "W.S.Q. homotopy" for "chain homotopy" in l. 6, 8, 15, 17, 18, 9b, "S.Q. homotopy" for "chain homotopy" in l. 3b.

p. 59. Read "S.Q. homotopy" for "chain homotopy" in l. 1, 2b. Insert between l. 5-6 "$\bar{x}'_{q(i)}(\eta_1 \cdots \eta_{p-1} \otimes \sigma_{q(i)-p}) = 0$ for $\sigma_{q(i)-p} \in K_{q(i)-p}$."

p. 60. Read "S.Q. homotopy classes" for "chain homotopy classes" in l. 12, "S.Q. homotopies" for "chain homotopies" in l. 16, and "W.S.Q. homotopies between the W.S.Q. homotopic maps" for "chain homotopies between the chain homotopic maps" in l. 18.

p. 61. Read "S.Q. homotopy" for "chain homotopy" in l. 9, 4b, and "W.S.Q. homotopic" for "chain homotopic" in l. 7b.

p. 62. Read "S.Q. homotopy" for "chain homotopy" in l. 4b.

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Correction: **Semicubical theory on higher obstruction**

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p. 17. Read "W.S.Q. homotopic" for "homotopic" in l. 13, and "W.S.Q. homotopies" for "chain homotopies" in l. 16.