

6. *The Universal Theorem.* We add d and f each three times, 7^9 twice, and n^9 ($n=8-13, 15$) each once, as in Theorem 10, this Bulletin (vol. 39 (1930), p. 710), and find that 140 powers suffice from h to $L_0=58221534000$. By Theorem 12, *ibid.*, page 711, with $t=841$, we find that 981 powers suffice from h to L_t , where $\log \log L_t=43.356$. By R. D. James' recent work for odd powers, every integer $>C$ is a sum of 981 ninth powers if $\log C=43.198$. Since $L_t > C$, we have the following result.

THEOREM 3. *All integers $\geq 2d+f$ are sums of 981 ninth powers.*

By (1_i) the integers ≥ 0 and $< b$ are $x+ya$ ($x \leq 511, y \leq 37$) and $z+38a$ ($z \leq 226$), and hence are sums of 548 powers. Adding b thirteen times, we see that 561 suffice to $14b$ and hence beyond c . Adding c seven times, we see that 568 suffice to $8c > d$. Adding d five times, we see that 573 suffice to $6d > f$. Hence 575 suffice to $2d+f$.

THEOREM 4. *Every positive integer is a sum of 981 ninth powers.*

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A NOTE

BY R. L. PEEK, JR.

M. Maurice Fréchet, of the University of Paris, has informed me that Cantelli published the following inequality in the *Bollettino dell' Associazione degli Attuari Italiani* (Milan, 1910):

$$P_{|X-Y|} \geq \epsilon \geq \frac{M_{2r} - M_r^2}{(\epsilon^r - M_r)^2 + M_{2r} - M_r^r},$$

where M_r is the mean of $|X-Y|^r$. As Fréchet pointed out in his letter to me, this inequality includes as a particular case ($Y=\bar{X}$, $\epsilon=t\sigma$, $r=1$) the inequality (2) given in my paper, *Some new theorems on limits of variation*, published in this Bulletin, December, 1933.

The journal in which Cantelli's paper appeared is not, so far as I have been able to ascertain, available in New York City.

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