# THE ANNALS of

# **STATISTICS**

# AN OFFICIAL JOURNAL OF THE INSTITUTE OF MATHEMATICAL STATISTICS

Articles	
P	AGE
A statistical theory of calibration	1
Convergence of estimates under dimensionality restrictionsL. LECAM	38
On the centering of a simple linear rank statisticWassily Hoeffding	<b>5</b> 4
Limiting distributions of Kolmogorov-Smirnov type statistics under the alternative	67
The conditional probability integral transformation and applications to obtain composite chi-square goodness-of-fit tests	
FEDERICO J. O'REILLY AND C. P. QUESENBERRY	74
Covariance stabilizing transformations	84
An empirical Bayes approach to multiple linear regressionSerge L. Wind	93
Differential equations and optimal choice problemsAnthony G. Mucci	104
Characterizations of populations using regression propertiesF. S. Gordon	114
Short Communications	
On a minimax estimate for the mean of a normal random vector under a generalized quadratic loss function	127
Asymptotically efficient estimation of covariance matrices with linear structure	135
Generalized Bayes minimax estimators of the multivariate normal mean with unknown covariance matrix PI-ERH LIN AND HUI-LIANG TSAI	142
Convergence of reduced empirical and quantile processes with application to functions of order statistics in the non-i.i.d. case	
GALEN R. SHORACK	146
Convergence rates for $U$ -statistics and related statistics	4
WILLIAM F. GRAMS AND R. J. SERFLING	153
Noncentral convergence of Wald's large-sample test statistic in exponential families	161
An asymptotic UMP sign test in the presence of tiesJ. Krauth	166
Continued on back of	oner.

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