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Meeting No.	Place	Date	Abstract Deadline*	Joint With
124	Dallas, Texas (Central Regional)	April 8-10, 1970	February 17, 1970	ASA
125	Chapel Hill, N.C. (Eastern Regional)	May 5-7, 1970	March 16, 1970	ASA, ENAR
126	Laramie, Wyoming (Annual Meeting)	August 25-28, 1970	July 6, 1970	AMS
127	Hanover, West Germany (European Regional)	August 19-26, 1970	June 30, 1970	
	University Park, Penn. (Eastern Regional)	April 21-23, 1971		ASA, ENAR
	Columbia, Missouri (Central Regional)	Spring, 1971		
	Ames, Iowa (Central Regional)	Spring, 1972		ASA, ENAR

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\* Abstracts should be submitted in duplicate to the Managing Editor, K. J. C. Smith, Department of Statistics, University of North Carolina, Chapel Hill, North Carolina 27514, on abstract blanks which may be obtained from him. Abstracts of papers to be presented *in person* at the meetings must be received on or before the corresponding deadline. Only one contributed paper may be given in person at any one meeting. Abstracts contributed by title may be submitted at any time and will be printed in the next issue to go to press. Abstracts should not exceed 200 words and should avoid displayed expressions and complicated formulae. They can be accepted from non-members of the IMS only if introduced by members. Abstracts must follow the stylistic requests on the abstract blank or they may be returned.