

THE ANNALS of MATHEMATICAL STATISTICS

FOUNDED AND EDITED BY H. C. CARVER, 1930-1938
EDITED BY S. S. WILKS, 1938-1949

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The title should be descriptive but concise, i.e. it should indicate the topic of the paper as clearly as possible but every word in it ought to be pertinent.

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Meet- ing No.	Place	Date	Abstract Deadline*	Joint With
	University Park, Penn. (Eastern Regional)	April 21-23, 1971	February 25, 1971	ASA, ENAR
	Columbia, Missouri (Central Regional)	May 5-7, 1971	March 4, 1971
	Fort Collins, Colorado (Annual)	August 23-26, 1971	June 24, 1971	ASA
	Ames, Iowa (Central Regional)	Spring, 1972		ASA, ENAR
	Blacksburg, Virginia (Eastern Regional)	Spring, 1972		

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