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Meet- ing No.	Place	Date	Abstract Deadline*	Joint With
132	Blacksburg, Virginia (Eastern Regional)	April 17-29, 1972	February 16, 1972	ASA
133	Ames, Iowa (Central Regional)	April 26-28, 1972	February 16, 1972	ASA, ENAR
134	Seattle, Washington (Western Regional)	June 19-21, 1972	April 19, 1972	
135	Montreal, Canada (Special Eastern Regional)	August 13-17, 1972	June 14, 1972	
136	Hanover, New Hampshire (Annual)	August 28-31, 1972	June 14, 1972	AMS
	Ithaca, New York (Eastern Regional)	Spring 1973		ASA, ENAR
	Albuquerque, New Mexico (Western Regional)	Spring 1973		

* Abstracts should be submitted in duplicate to the Executive Secretary on abstract blanks which may be obtained from him. Abstracts of papers to be presented *in person* at the meetings must be received on or before the corresponding deadline. Only one contributed paper may be given in person at any one meeting. Abstracts contributed by title may be submitted at any time and will be printed in the next issue to go to press. Abstracts should not exceed 200 words and should avoid displayed expressions and complicated formulae. They can be accepted from non-members of the IMS only if introduced by members. Abstracts must follow the stylistic requests on the abstract blank or they may be returned.