

Correction to "On Fitting's lemma"

Yasuyuki HIRANO

(Received February 6, 1980)

In Proposition 1 in [1] the proof of $1) \Rightarrow 2)$ is invalid, since $\text{End}((R^n/e_{11}K)_R)$ is not ring isomorphic to $I_{(R)_n}(K)/K$ in general. Here is a revised proof.

PROOF OF $1) \Rightarrow 2)$ OF [1, Proposition 1]. Let K be a right ideal of $(R)_n$. Then each element $s \in I_{(R)_n}(K)$ induces, by left multiplication, an $(R)_n$ -endomorphism of the right $(R)_n$ -module $(R)_n/K$, which we denote by $f(s)$. It is easy to see that the ring $I_{(R)_n}/K$ is isomorphic to the subring $\text{End}_{(R)_n}((R)_n/K)$ of $\text{End}_R((R)_n/K)$ by the map $s + K \rightarrow f(s)$. Suppose $xy - 1 \in K$ with $x \in I_{(R)_n}(K)$ and $y \in (R)_n$. Then $f(x)$ is a surjective endomorphism and hence an isomorphism by 1). If the inverse of $f(x)$ is represented by $f(z)$ with $z \in I_{(R)_n}(K)$, we have that $zx - 1 \in K$. Since $y - z = z(xy - 1) - (zx - 1)y \in K$, it is immediate that $y \in I_{(R)_n}(K)$ and $yx - 1 = (y - z)x - (zx - 1) \in K$.

The author is grateful to Prof. J. W. Fisher for pointing out the error.

Reference

- [1] Y. Hirano: On Fitting's lemma, *Hiroshima Math. J.* **9** (1979), 623–626.

*Department of Mathematics,
Faculty of Science,
Hiroshima University*

