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The proof of Theorem 2 was misleaded. We give following proof. The uniform convergency of the series

$$\sum \frac{a_\nu}{\nu} \frac{\sin \nu t}{t}$$

in the interval $0 < \varepsilon \leqq t \leqq 2\pi - \varepsilon$, is evident from (7). We write

$$\sum_{\nu=1}^{\infty} \frac{a_\nu}{\nu} \frac{\sin \nu t}{t} = \sum_{\nu=1}^{n} + \sum_{\nu=n+1}^{\infty} = u_1(t) + u_2(t),$$

say, where $n = [t^{-\frac{1}{\alpha}} \varepsilon^{-\frac{1}{\alpha}}]$. Then

$$|u_2(t)| \leqq t^{-1} \sum_{\nu=n+1}^{\infty} \left| \frac{a_\nu}{\nu} \right| = O(t^{-1} n^{-\alpha}) \leqq \varepsilon.$$

Applying Abel's transformation twice to $u_1(t)$, we get

$$u_1(t) = \sum_{\nu=1}^{n-1} a_\nu \frac{\sin \nu t}{\nu t} = \frac{1}{t} \left(\sum_{\nu=1}^{n} S_\nu \, \Delta_\nu^2(t) + S_{n-1} \Delta_n(t) + s_n \frac{\sin nt}{n} \right)$$

where

$$\Delta_n(t) = \frac{\sin nt}{n} - \frac{\sin(n+1)t}{n+1}, \quad \Delta_n^2(t) = \Delta(\Delta_n t).$$

Since we have easily

$$\Delta_n(t) = O\left(\frac{t}{n}\right), \qquad \Delta_n^2(t) = O\left(\frac{t^2}{n}\right),$$

$$|u_1(t)| = \frac{1}{t} \left\{ \sum_{\nu=1}^{n-1} o(\nu^\alpha) \left(\frac{t^2}{\nu}\right) + o(n^\alpha) \left(\frac{t}{n}\right) + O(n^{1-\alpha}(n^{-1})) \right\}$$

$$= o(t \cdot n^\alpha) + o(n^{\alpha-1}) + O(n^{-\alpha} t^{-1})$$

$$= o(1) + o(1) + \varepsilon = o(1).$$

Thus we have the desired results.