

**CORRIGENDUM TO “ON THE CARTIER DUALITY OF
CERTAIN FINITE GROUP SCHEMES OF ORDER p^n , II”
[Tsukuba J. Math. 37 (2) (2013) 259–269]**

By

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Abstract. We correct an error of the proof of Lemma 1 in the author’s paper [1]. Also a typographical error is corrected.

There is an error in the proof of Lemma 1 in [1], which is amended as follows.

On Page 266, line –3, it is claimed that the diagram there given were commutative. But it is false. The only consequence of this wrong claim that is used in the subsequent argument is the inclusion

$$\text{Ker}(F^{(\lambda)} \circ T_a) \subset \text{Ker}(F^{(\lambda^{p^\ell})}).$$

See Page 267, line 2. Therefore, one has only to reprove this inclusion.

Suppose $\mathbf{x} \in \text{Ker}(F^{(\lambda)} \circ T_a)$, or equivalently,

$$(C1) \quad \Phi_{k+1}(T_a(\mathbf{x})) = \lambda^{p^k(p-1)}\Phi_k(T_a(\mathbf{x})), \quad k \geq 0.$$

See Page 265, line –8. To show $\mathbf{x} \in \text{Ker}(F^{(\lambda^{p^\ell})})$, we wish to prove the equivalent

$$(C2) \quad (\Phi_k(F^{(\lambda^{p^\ell})}(\mathbf{x})) =)\Phi_{k+1}(\mathbf{x}) - \lambda^{p^{\ell+k}(p-1)}\Phi_k(\mathbf{x}) = 0, \quad k \geq 0$$

by induction on k .

Suppose $k = 0$. The desired equality then follows by direct computation using Eqs. (5) and (7) on Page 265.

Suppose $k > 0$. The induction hypothesis $\Phi_i(F^{(\lambda^{p^\ell})}(\mathbf{x})) = 0$, $0 \leq i < k$, immediately implies

$$(C3) \quad \Phi_{i+1}(\mathbf{x}) = \lambda^{p^\ell(p^{i+1}-1)}\Phi_0(\mathbf{x}), \quad 0 \leq i < k.$$

Using (5) again, we compute

$$\begin{aligned}
 \Phi_{k+1}(T_a(\mathbf{x})) &= a_0^{p^{k+1}} \Phi_{k+1}(\mathbf{x}) + pa_1^{p^k} \Phi_k(\mathbf{x}) + \cdots + p^{k+1} a_{k+1} \Phi_0(\mathbf{x}) \\
 &= a_0^{p^{k+1}} \Phi_{k+1}(\mathbf{x}) + (p^\ell \lambda^{p^{k+1}} / \lambda^{p^\ell}) \\
 &\quad \times \left\{ (p^{(\ell-1)(p^k-1)} \alpha_1^{p^k} + \cdots + p^{(\ell-k)(p-1)} \alpha_k^p) \right. \\
 &\quad \left. + 1 - p^{(p^{k+1}-1)\ell} - \sum_{i=1}^k p^{(p^{k+1-i}-1)(\ell-i)} \alpha_i^{p^{k+1-i}} \right\} \Phi_0(\mathbf{x}) \\
 &= a_0^{p^{k+1}} \Phi_{k+1}(\mathbf{x}) + \{ (p^\ell \lambda^{p^{k+1}} / \lambda^{p^\ell}) - (p^\ell \lambda^{p^{k+1}} / \lambda^{p^\ell}) \} \Phi_0(\mathbf{x}).
 \end{aligned}$$

Similarly we have $\Phi_k(T_a(\mathbf{x})) = (p^\ell \lambda^{p^k} / \lambda^{p^\ell}) \Phi_0(\mathbf{x})$. The last two results, combined with (C1), show that the equality (C3) holds when $i = k$, as well. The equalities (C3) for $i = k - 1, k$ show the desired (C2).

There is a misprint in [1]. On page 268, line -2 should read “ $E_p(\mathbf{z}, \lambda^{p^\ell}; \psi^{(\ell)}(x))$ ” instead of “ $E_p(\mathbf{z}, \lambda; \psi^{(\ell)}(x))$.”

Reference

- [1] M. Amano, On the Cartier duality of certain finite group schemes of order p^n , II, Tsukuba J. Math. **37** (2013), no. 2, 259–269.

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