

THE RULE OF EXCISION IN POSITIVE IMPLICATION

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The point made in [1] that the rule of excision

RE: $\vdash \alpha, \vdash \phi (C \alpha \beta) \rightarrow \vdash \phi (\beta)$

can be more powerful than the rule of detachment

RD: $\vdash \alpha, \vdash C \alpha \beta \rightarrow \vdash \beta$

is to be made with great economy in the context of positive implication. Assuming **RE**, substitution and the axiom

1. $CCpCqrCCpqCpCsr$

we have

*2. $CCpCqrCCpqCpr$ [1 *s*/1, **RE**]

3. $CCqrCqCsr$ [1 *p*/1, **RE**]

*4. $CrCsr$ [3 *q*/1, **RE**]

and **RD** as a special case of **RE**, thus having the positive system. But the matrix **MI**

MI	C	0	1	2
	*0	0	1	1
	1	0	0	1
	2	0	0	0

MII	C	0	1	2
	*0	0	2	2
	1	0	2	0
	2	0	0	0

which is hereditary under **RD**, verifies 1 and rejects 2;

$$CC1C12CC11C12 = CC11C01 = C0C01 = 1.$$

If interest of the system is disregarded, the point can be proved with maximum economy by excising *s* from 4 to obtain 5. *Crr*; but the matrix **MII** shows that 5 is independent of 4 and **RD**.

REFERENCE

[1] Angell, R. B., The sentential calculus using rule of interference R_e , *The Journal of Symbolic Logic*, vol. 25 (1960), p. 143.

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