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Articles

Multivariate generalizations of the Wald-Wolfowitz and Smirnov two-sam-	
ple tests Jerome H. Friedman and Lawrence C. Rafsky	697
Predictive likelihood DAVID HINKLEY	718
Estimation of starshaped sequences of Poisson and normal means Moshe Shaked	729
Conditional properties of statistical procedures G. K. Robinson	742
Conditional properties of statistical procedures for location and scale	
parameters G. K. Robinson	756
Erdos-Rényi laws Sándor Csörgő	772
Erdős-Rényi laws Sándor Csörgő Asymptotic normality of permutation statistics derived from weighted sums	
of bivariate functions C. P. SHAPIRO AND LAWRENCE HUBERT	788
A convergence theorem for random linear combinations of independent	
normal random variables N. Christopeit and K. Helmes	795
Time series prediction functions based on imprecise observations	
LAWRENCE PEELE AND GEORGE KIMELDORF	801
A coordinate-free approach to finding optimal procedures for repeated	
measures designs Steven F. Arnold	812
measures designs	
tivariate normal patterned mean and covariance matrix testing	
problem	823
Minimax estimation of a normal mean vector when the covariance matrix	
is unknown Leon Jay Gleser	838
A reduction theorem for certain sequential experiments. II L. LE CAM	847
A stepwise Bayesian procedure Francis C. Y. Hsuan Characterization of a family of distributions by the independence of size	860
Characterization of a family of distributions by the independence of size	
and shape variables	869
A characterization of the uniform distribution on the circle	
J. T. Kent, K. V. Mardia and J. S. Rao	882
Empirical Bayes estimation in Lebesque-exponential families with rates	
near the best possible rate R. S. SINGH Calculation of univariate and bivariate normal probability functions D. R. DIVGI	890
Calculation of univariate and bivariate normal probability functions D. R. Divgi	903
Systems with exponential life and IRFA component lives	
HENRY W. BLOCK AND THOMAS H. SAVITS	911
Short Communications	
Note on a result of Seeger in partitioning normal populations GWENDA J. CANE	917
Confidence bands for Kaplan-Meier	920
Notes	
-10000	
Correction to "On theory and application of BIB designs with repeated	005
blocks" W. FOODY AND A. HEDAYAT Correction to "On invariant tests of uniformity for directions and orienta-	925
Correction to On invariant tests of uniformity for directions and orienta-	000
Acknowledgement of priority to "A characterization of the von Mises	926
distribution" A characterization of the von Mises LOUIS CORDON AND MALCOLM HUDSON	997

Vol. 7, No. 4—July 1979

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[5] Wilks, S. S. (1938). The large-sample distribution of the likelihood ratio for testing composite hypotheses. Ann. Statist. 1 60-62.

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