# THE ANNALS of STATISTICS

# AN OFFICIAL JOURNAL OF THE INSTITUTE OF MATHEMATICAL STATISTICS

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The Annals of Statistics, Volume 4, Number 6, November 1976. Published bimonthly in January, March, May, July, September, and November by The Institute of Mathematical Statistics, IMS Business Office, 3401 Investment Blvd., Suite 6, Hayward, California 94545.

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thus, 
$$(a + b)/(c + d)$$
 is preferred to  $\frac{a+b}{c+d}$ , and

$$(2\pi)^{-1}$$
 or  $1/(2\pi)$  to  $\dfrac{1}{2\pi}$  . Also,  $a^{b(\epsilon)}$  and  $a_{b(\epsilon)}$  are pre-

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[5] Wilks, S. S. (1938). The large-sample distribution of the likelihood ratio for testing composite hypotheses. *Ann. Statist.* 1 60-62.

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