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DISCUSSION OF "SPATIAL ACCESSIBILITY OF PEDIATRIC PRIMARY HEALTHCARE: MEASUREMENT AND INFERENCE"

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This paper describes the infusion of many fresh statistical ideas into the area of spatial access to healthcare, and I hope that the procedures described are widely implemented. What is described is a large and an impressive applied research project incorporating space-varying coefficient models, simultaneous confidence bands and backfitting to address otherwise potentially unstable and computationally expensive estimation. In my opinion, there are three high-level areas of this work that would benefit from further development. I describe these next, followed by much briefer descriptions of some minor quibbles I have with the paper that the authors may want to consider.

The first area where further development could be valuable is in the "procedure developed to systematically evaluate multiple models." I commend the authors in not narrowing down the space of possible models to a single "best" model and instead considering a family of acceptable models. I also appreciate that they state clear and reasonable criteria for deeming models to be acceptable. What I find less satisfying is that the procedure described to summarize the multiple models deemed to be acceptable is largely qualitative. Thus, the ability to make accurate probability statements about the relationships between the predictors and the outcome, over the family of acceptable models, is lost. The issues surrounding model selection and/or how to incorporate the information from a family of useful models into an inferential structure are highly relevant to any decision-making that could result from statistical modeling. This issue was highlighted in a recent National Research Council Report evaluating the existing research regarding deterrence and the death penalty in the U.S. [National Research Council (2012)]. The committee for that report, which I served upon, concluded that large model uncertainty swamped any claims of the presence or absence of statistical significance within any particular model. Bradley Efron's work, "Estimation and Accuracy After Model Selection," also presented at the 2014 Joint Statistical Meetings, may be useful to consider in this context [Efron (2013)].

In the particular setting of this spatial accessibility analysis, the model uncertainty issues are due to correlations among the predictors. This source of model uncertainty makes relationships of individual correlated predictors to outcomes of little value. A principal components or factor analysis may be helpful to better

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describe what the predictors are whose relationship with the outcome it would be useful to estimate.

The second direction for further development stems from a quite typical observation about optimization procedures of the sort described in Section 2: linear optimization procedures such as the one implemented here output quantities with no measures of uncertainty attached to them. The authors chose to address the sensitivity of the procedure's outputs (accessibility measures) to small variations in the constant values incorporated into the procedure rather than incorporating the uncertainty in those parameter estimates into the procedure such that they are propagated through to the outputs. I appreciate the authors' efforts in this direction, yet find it unsatisfying as there are two things we do not know: (1) whether small variations from the selected constant values for the parameters are a good measure of the uncertainty about the parameters and (2) how the uncertainty in many parameters collectively impacts the procedure's output.

There appear to be several sources of uncertainty impacting the outputs of the optimization procedure that it would be helpful to quantify; most of these are mentioned to some degree in the paper, although not in this context. The first source of uncertainty is that the algorithm does not have a unique solution and thus different runs of the procedure result in different output. Second, distance from each patient in a census tract to a doctor is approximated using the centroid of the census tract the patient lives in-this provides an estimate of the actual distance that would need to be traveled. Third, two of the bounds used in the optimization process vary at the individual doctor level, but data on them is available only at aggregated levels. The authors explore the sensitivity of the resulting spatial access measurements when they simulate individual draws of these parameters at the doctor level from the aggregate parameters. From this they establish that in most census tracts the impacts on the output of this uncertainty are small. Taken a step farther, this simulation exercise would allow them to propagate the uncertainty from this missing data through the procedure to the output. More generally, few of the parameters for which constant values were selected are observed or derived from meaningful thresholds and I would expect few to be constant in reality. For instance, the maximum number of patients that can be seen and the minimum number needed to sustain a doctor's practice seem likely to vary based on local operating costs and wages as well as upon the mix of reimbursement levels the doctor is receiving from their patient mix (and presumably correlated with the proportion of their patients with Medicaid coverage). This suggests that it would be useful to jointly estimate these parameters with the proportion of Medicaid patients in doctors' patient populations. If the variability is not incorporated into the optimization procedure, it would be useful to more systematically discuss the justification and consequences of this decision. In some cases this may be a complete normative argument, for example, all people should be able to have the same travel distance limit, and in others it would involve making a complete case for the assumptions that the variability is of a particular modest magnitude and that considering the variability of one parameter at a time is sufficient and then illustrating the impact of variations of that magnitude for each parameter on the outputs of the procedure.

The third area that could benefit from additional development is that it is unclear where the uncertainty quantified and used for making inferences in Section 3 of the paper comes from. As described in the paper, the optimization procedure results in measurements (with no uncertainty in them) of spatial access for the two groups of interest in every census tract in Georgia. This is a census with no sampling variability. Are the authors relying on a theoretical super population from which their data is drawn? If so, it would be useful to say so and describe the sampling method from the super population that they are assuming—what is sampled from that super population and how? Is there clustering? Or is there a different source of uncertainty than a sample from a super population?

In the remainder of this discussion I briefly describe a small set of quibbles with or remaining questions about the methods in this paper. While I do not question that spatial accessibility is important, I do not find it is clear that spatial accessibility is equally important to financial accessibility—driving a longer way or getting a ride do not necessarily seem comparable to having the ability to get the care paid for once you arrive. Regarding the policy simulations, there are limitations of the fixed nature of the optimization procedure. I am concerned that implementing a new policy, such as increasing the mobility of those with Medicaid insurance, impacts other parameters currently held fixed within the optimization under potential policy changes. In the example just given, greater access to transportation may also affect the probability that doctors farther from large concentrations of Medicaid patients accept any Medicaid patients and the proportion of their patient population they would allow to be Medicaid patients. Microsimulation models, such as are implemented in economics and other fields, may be helpful to consider, as they would allow the parameters to jointly vary. A second quibble regarding the policy simulations is that the authors state that they "target policies that are (approximately) Pareto optimal" but focus their discussion on the policies of reducing the probability that doctors accept any Medicaid patients or reducing the proportion of Medicaid patients doctors accept—neither of which can claim to be Pareto optimal. Regarding the initial optimization procedure, it seems that the authors are assuming all doctors provide equal quality of care for all patients and it would be helpful for there to be some discussion of this and how it could be relaxed. Last, I have a few remaining questions about the methods used. Regarding Section 3.3, given that there is no additional data regarding the distribution of the population within each census tract, why does the Kernel Density Estimator provide superior estimates to the simpler calculation of dividing the population by its land mass? Providing evidence of superior estimates could be useful. In Section 3.4, how is "consistency" defined? I do not understand how the Diversity Ratio is reported to have both constant and nonconstant shapes under different specifications and be consistent. Also in Section 3.4, what does it mean for a predictor which has a space-varying relationship with the outcome in all specifications to be summarized as having a statistically significant relationship with the outcome?

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